

AI-based prediction and control of tokamaks: Combining simulations and experimental data

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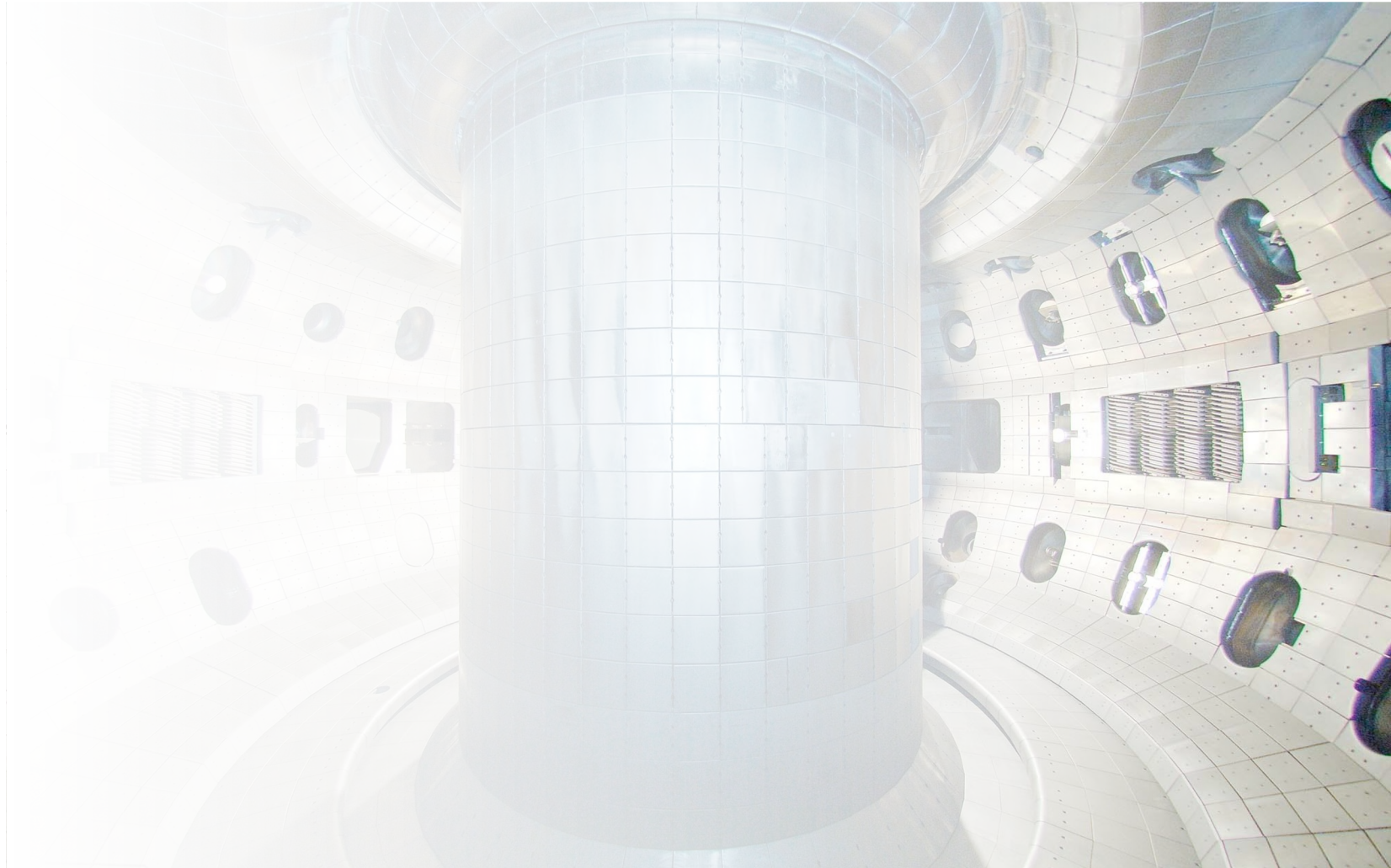
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Dissertation Defense

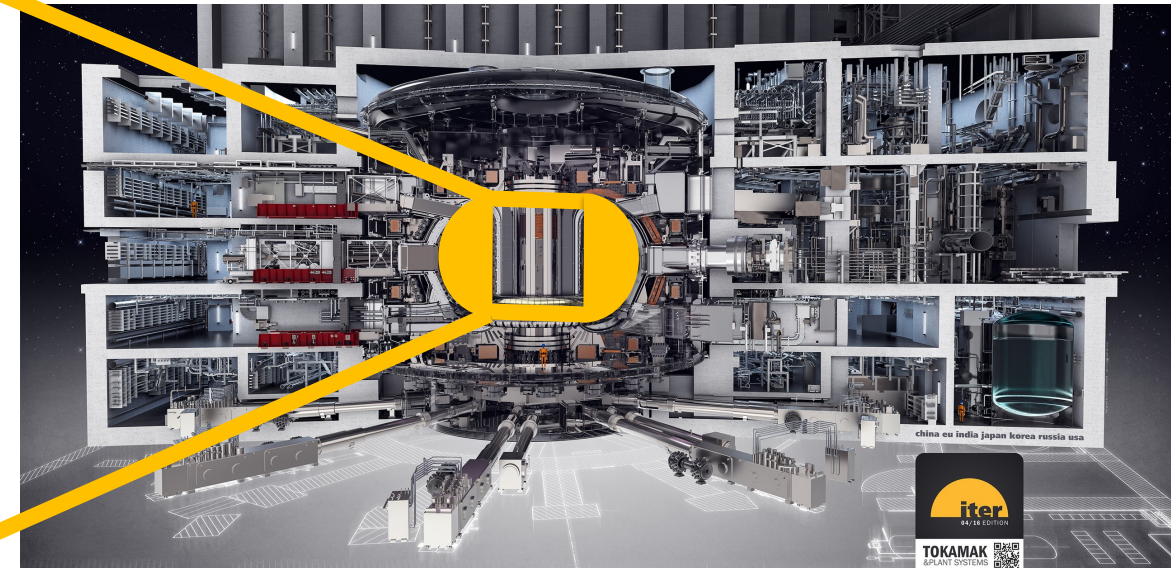
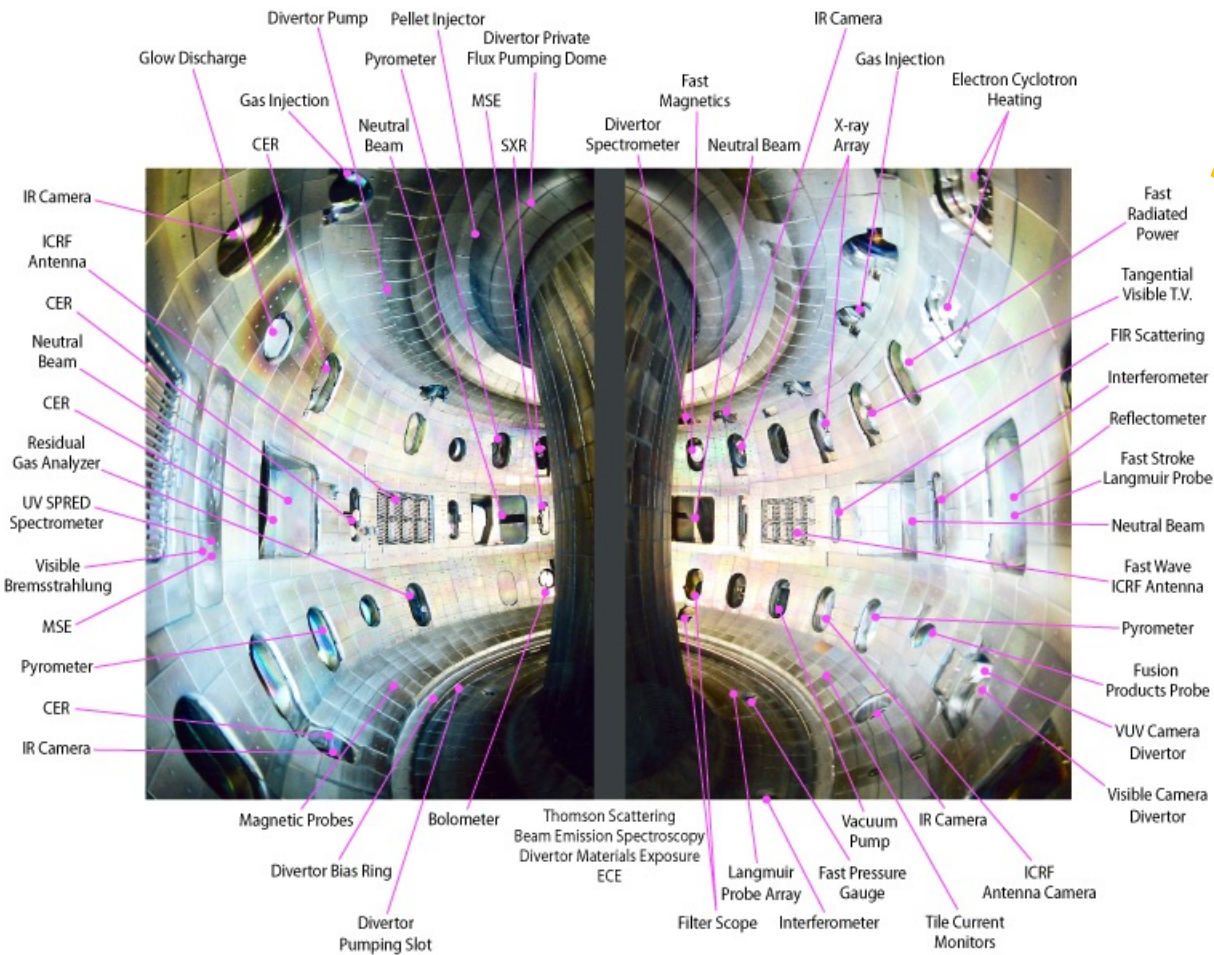
March 2024



Building and "driving" a tokamak reactor is wildly complex

- **\$B to build, \$M/day to operate**
- **~hundreds of control knobs, ~thousands of diagnostics (comparable to aircraft)**

Humphreys 2015, PoP 22 021806



Tokamak actuators (the knobs operators turn)

Power: 1kW → 1,000kW



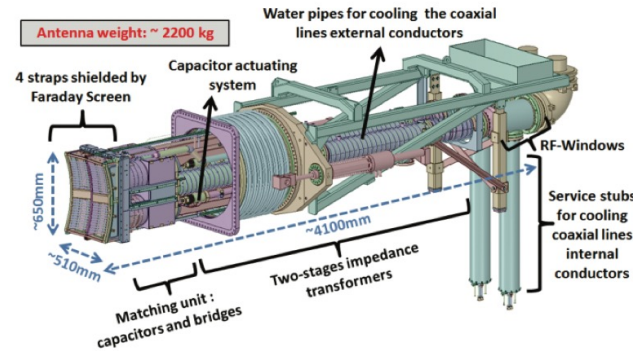
1. Add microwaves



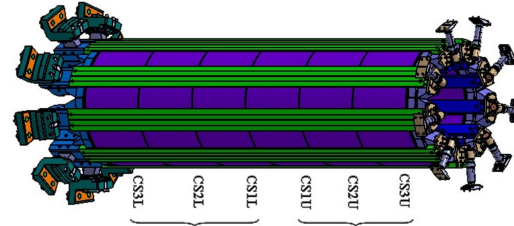
2. Apply electrical current



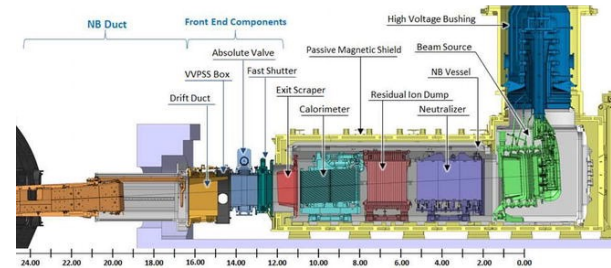
3. Add hot particles



Electron Cyclotron Heating (ECH)



Ohmic transformer



Neutral Beams

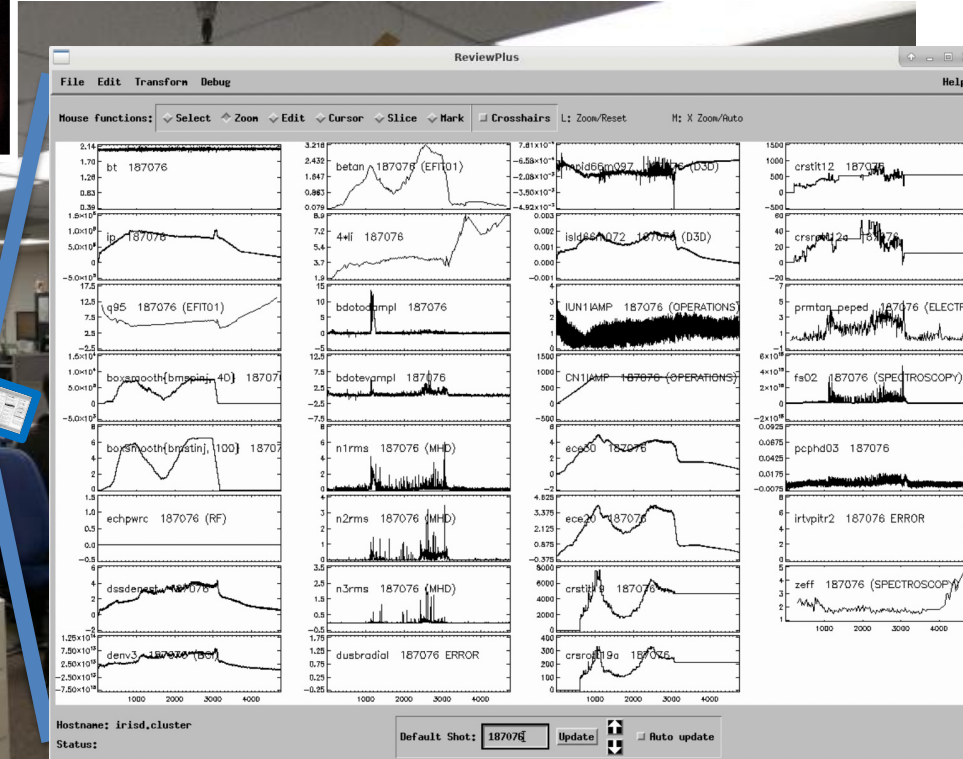
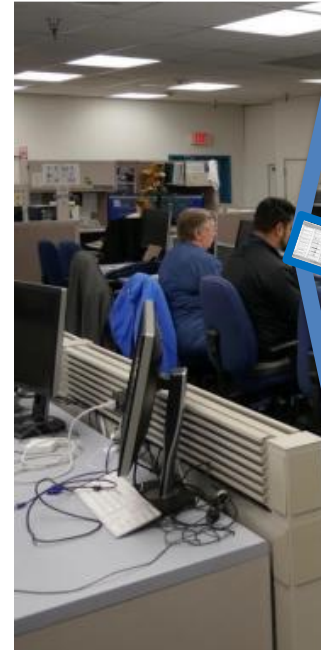
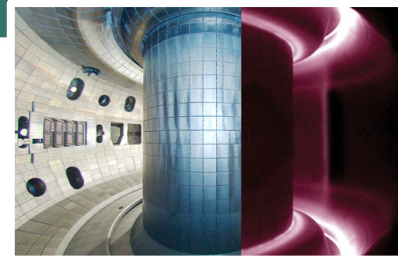
Reproducing and improving a discharge by trial-and-error

Experiment goal: reproduce and improve an experiment from 10 years before

“Many shots had MHD modes at 3 s... to try to improve that we changed Electron Cyclotron Heating deposition (180639-180642), and go to lower (180643-180646) and higher (180647) plasma current... none of which were successful.

We also tried lowering the voltage on the off-axis beams (180645) to get rid of the bursty modes and moving the BetaN ramp earlier (180646.)”

Ultimately, got “good reproduction of 133103, but no significant improvement”

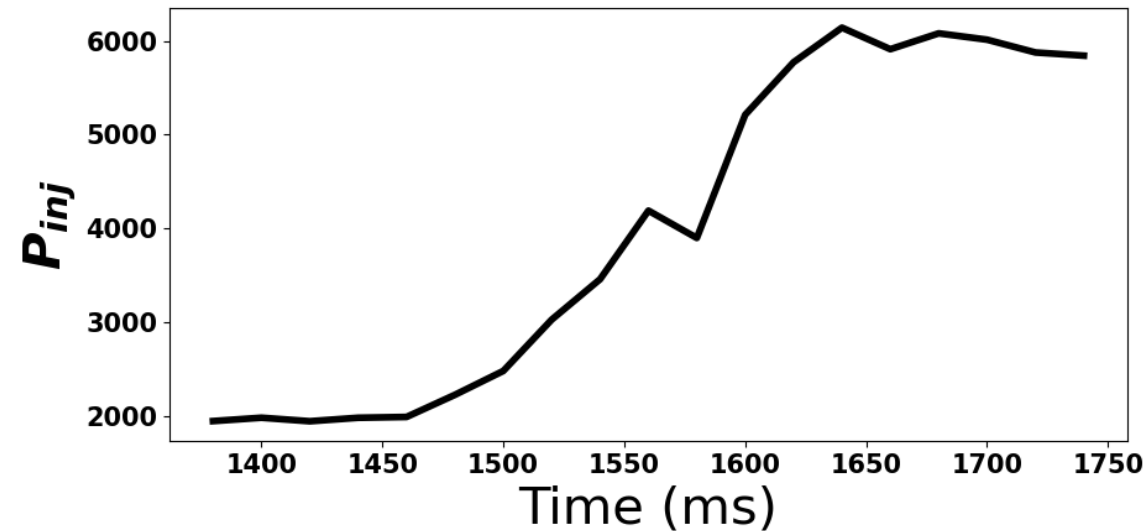
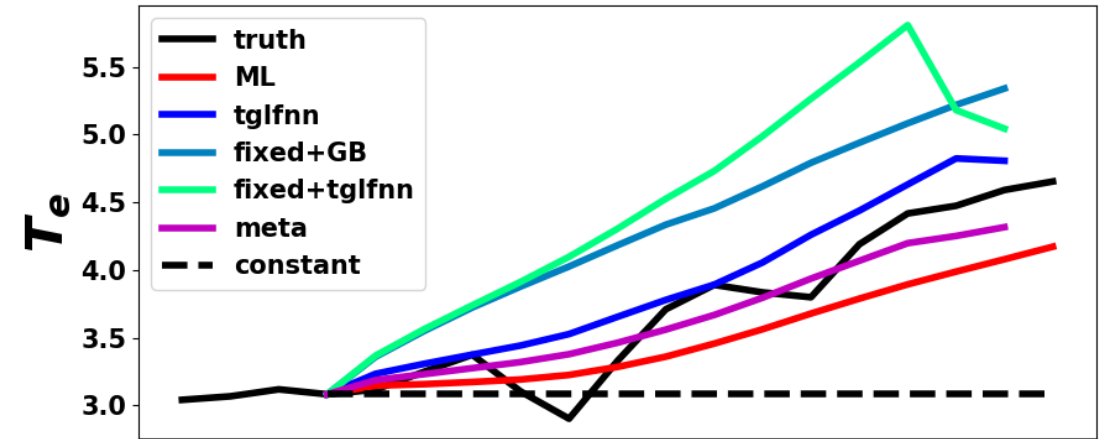


DIII-D Tokamak Control Room
Nik Logan's “overview” scope

Human operators combine simulations, heuristics, and experience to achieve desired state by trial-and-error

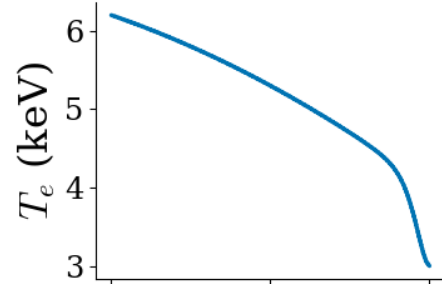
Combining simulations and experimental data for tokamak dynamics

- **Data-driven tokamak dynamics + control**
- **Validating analogous physics simulations**
- **Combining experimental data + simulations**

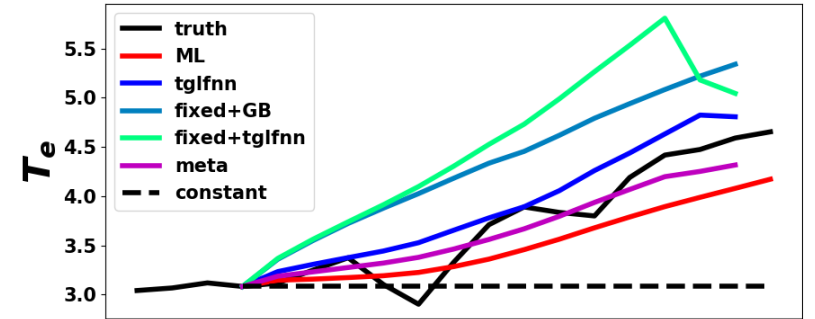


Kinetic plasma profile dynamics model

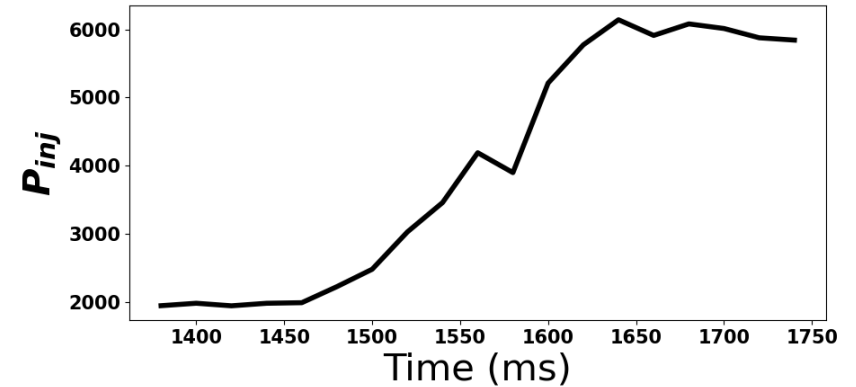
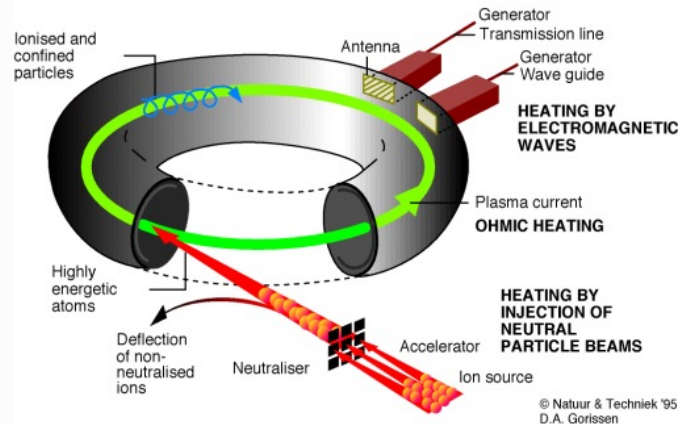
$x = \text{state}$
(1D profiles+shape)



$f = \text{mapping}$



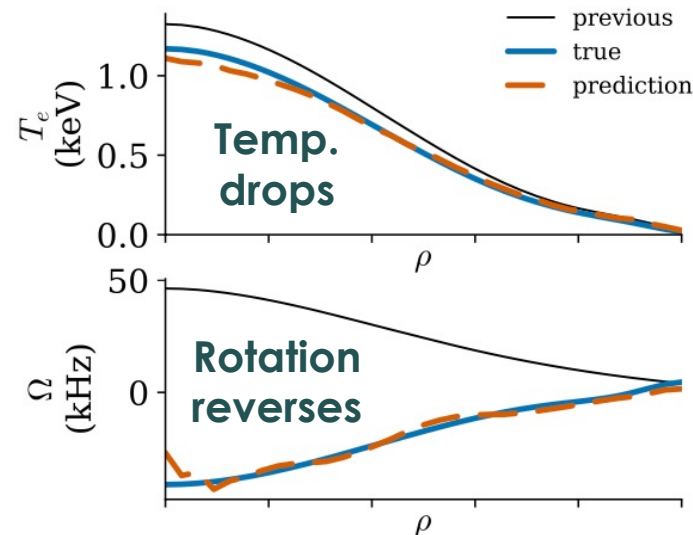
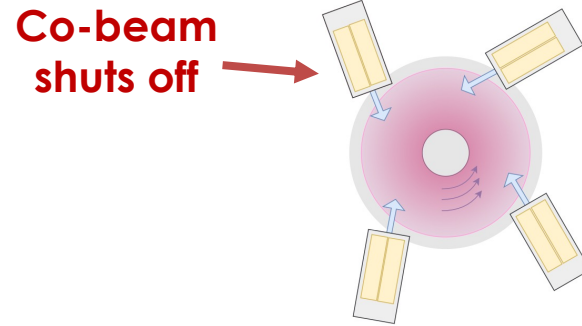
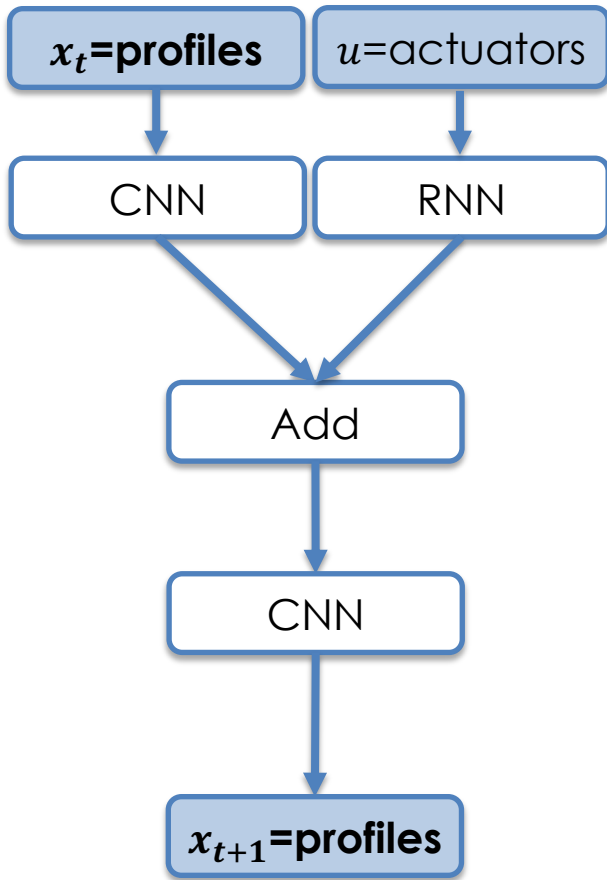
$u = \text{actuators}$



Find mapping f s.t. $x_{t+1} = f(x_t, u_t, u_{t+1})$

Built data-driven (neural net) profile predictor

Find mapping f s.t. $x_{t+1} = f(x_t, u_t, u_{t+1})$



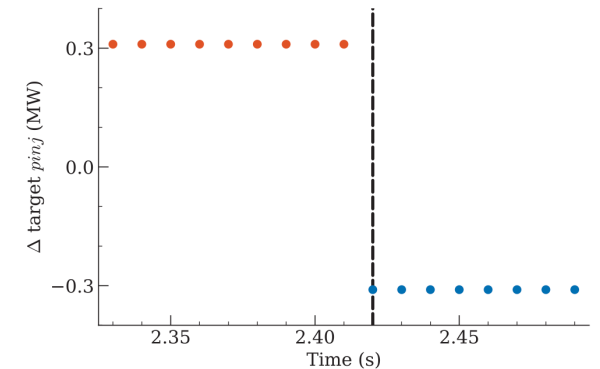
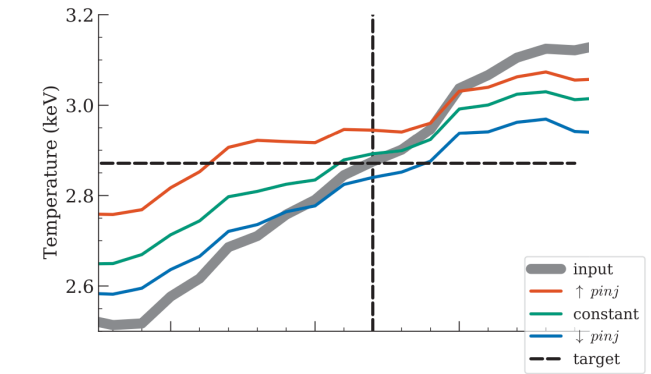
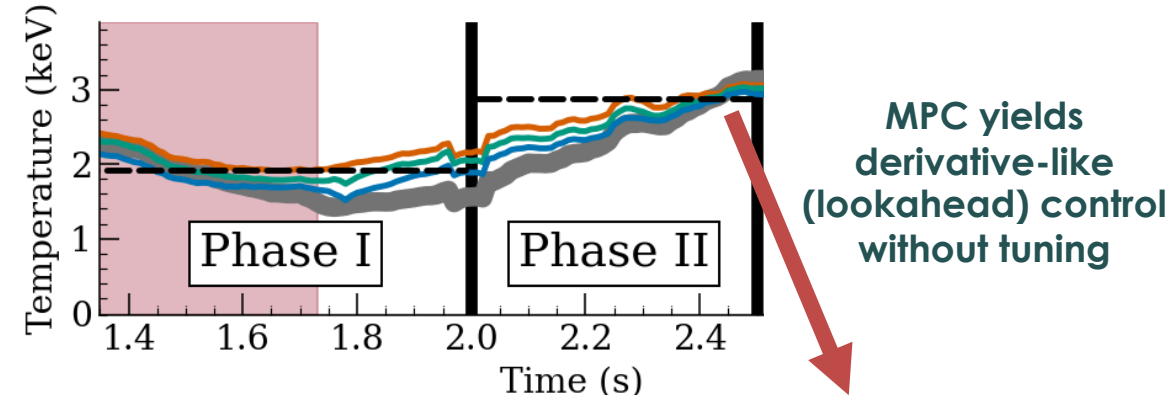
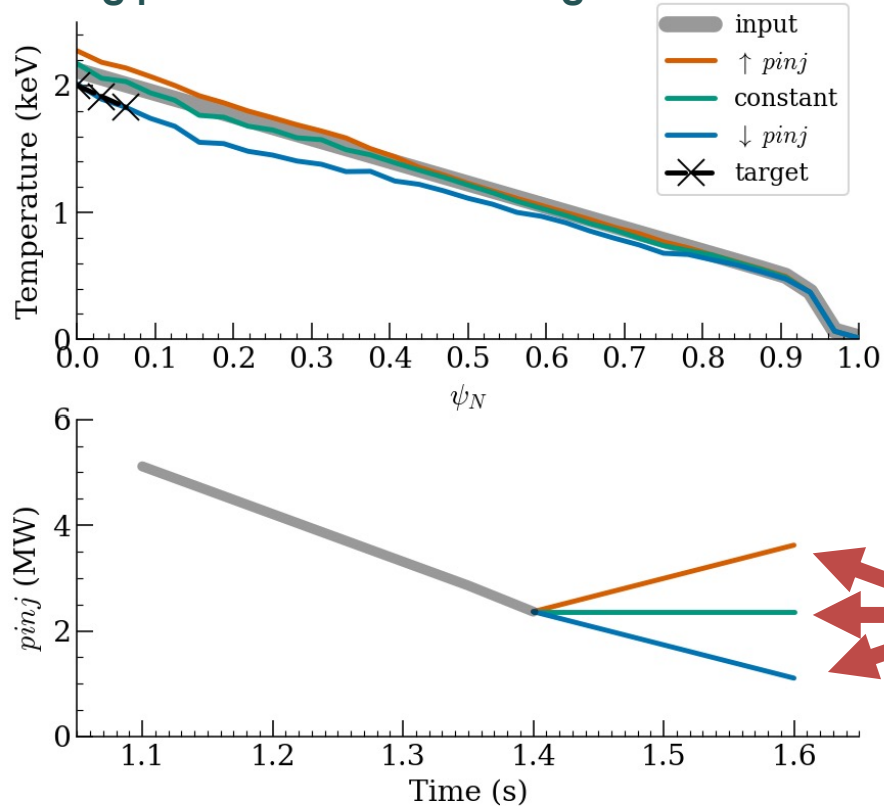
Abbate, Conlin Nuclear Fusion 2021

Profiles (x)	Source
Electron density	Thomson
Electron Temperature	Thomson
Ion temperature	CER
Ion velocity	CER
q	EFIT01
Impurity density	CER

Actuators (u)
NB Power
NB Torque
Target I _p
Gas flow rates
[Shape parameters]
[ECH]

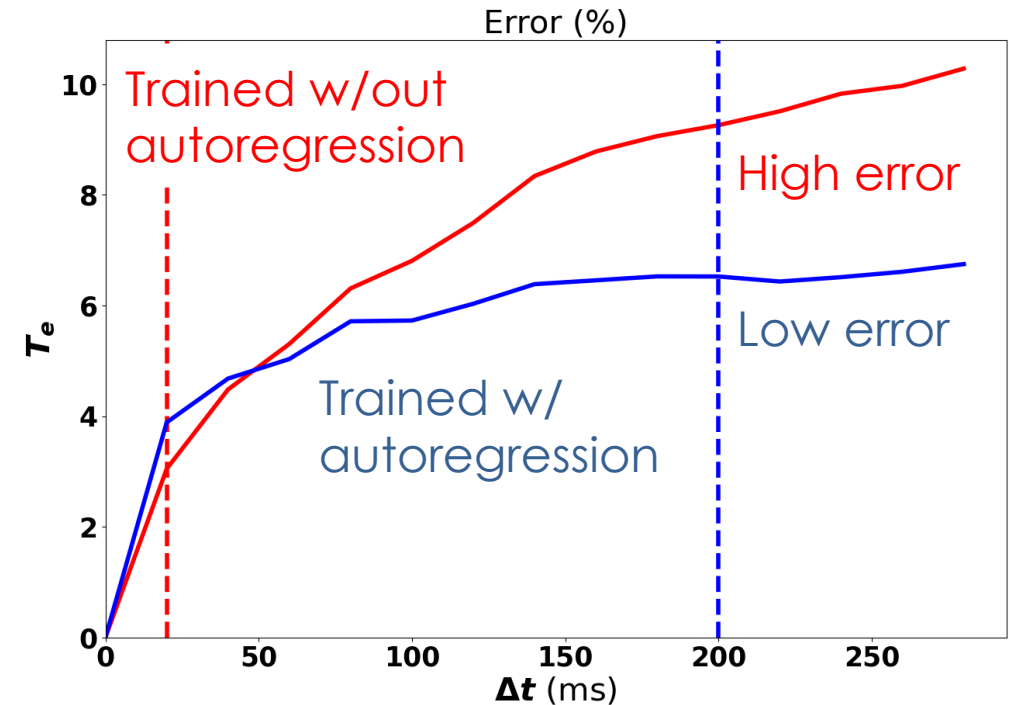
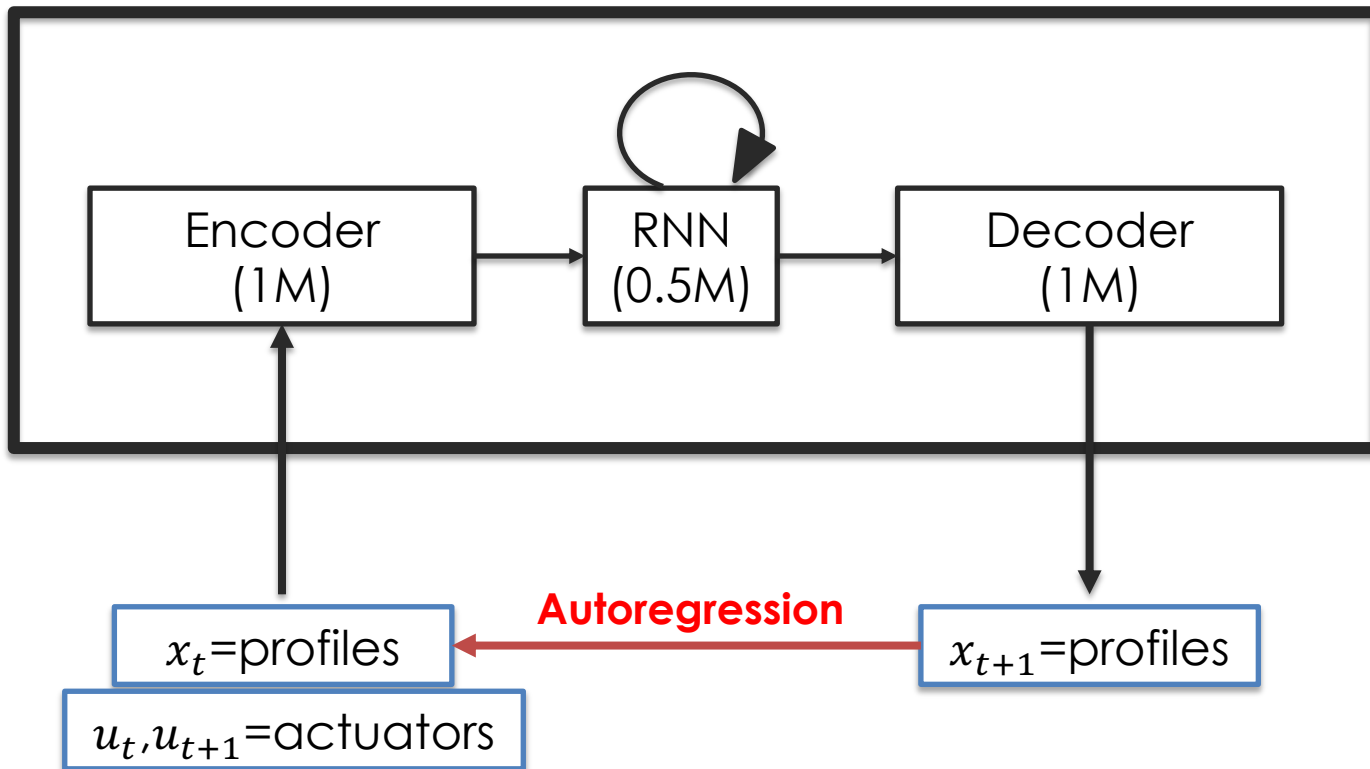
Neural network profile control in PCS (starting w/ finite set MPC)

Controller chooses control option yielding prediction closest to target



New architecture and training methodology to predict autoregressively

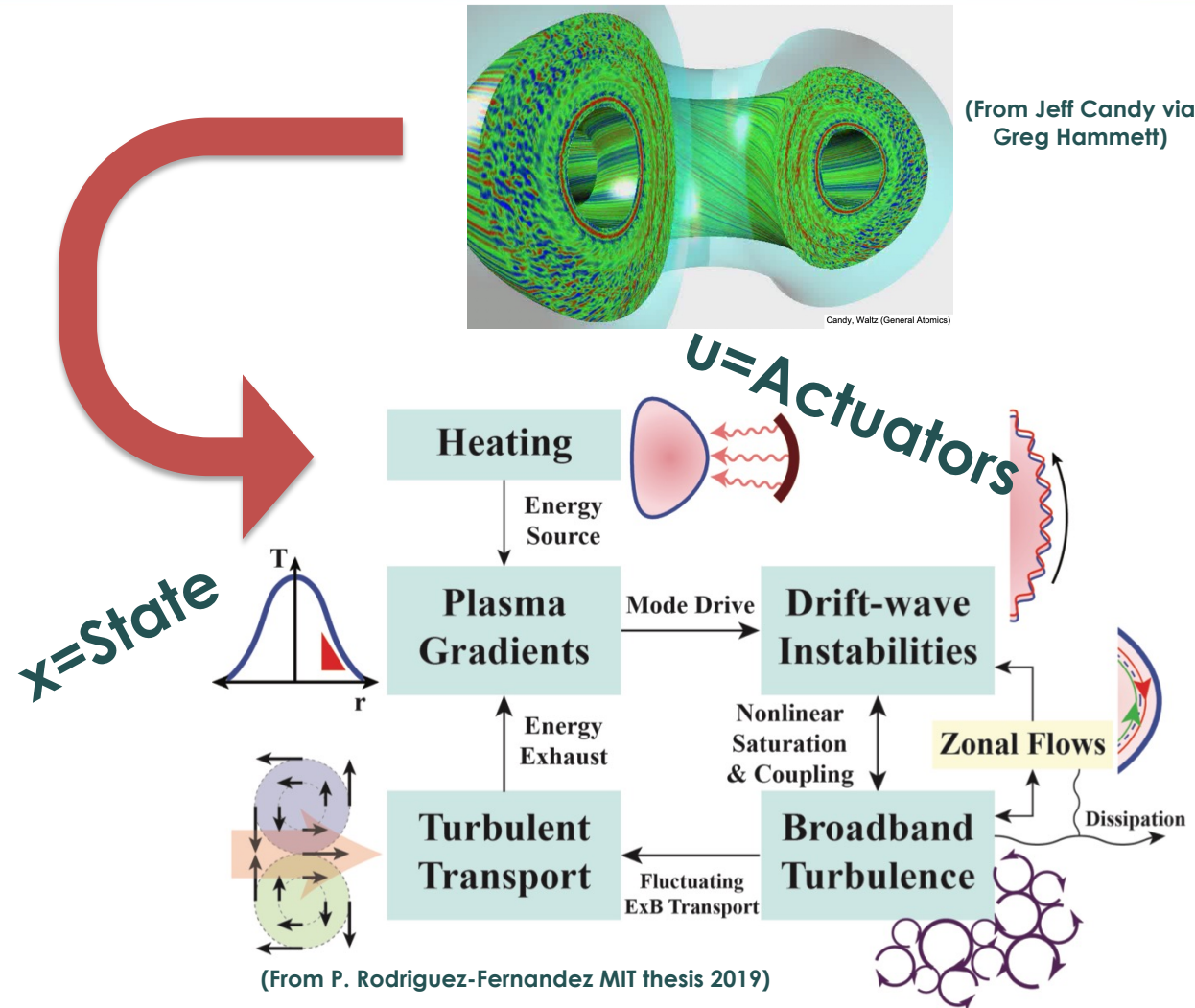
- **New architecture allows continuous predictions any step in future (Char, CMU), via autoregression**
- **Additionally training model with autoregression allows tuning model for any time horizon**



Find mapping f s.t.
$$x_{t+1} = f(x_t, u_t, u_{t+1})$$

Our approximate plasma state: 1D profiles

- **Goal: track $\sim 10^{23}$ particles through 6D phase space w/ nonlocal interactions**
 - Massive progress made (over ~ 70 yrs + $\sim 1,000$ careers)
 - Find approximations that fit data, try to avoid overfitting
- **Simplified plasma state given by 1D profiles \rightarrow “integrated modeling”**

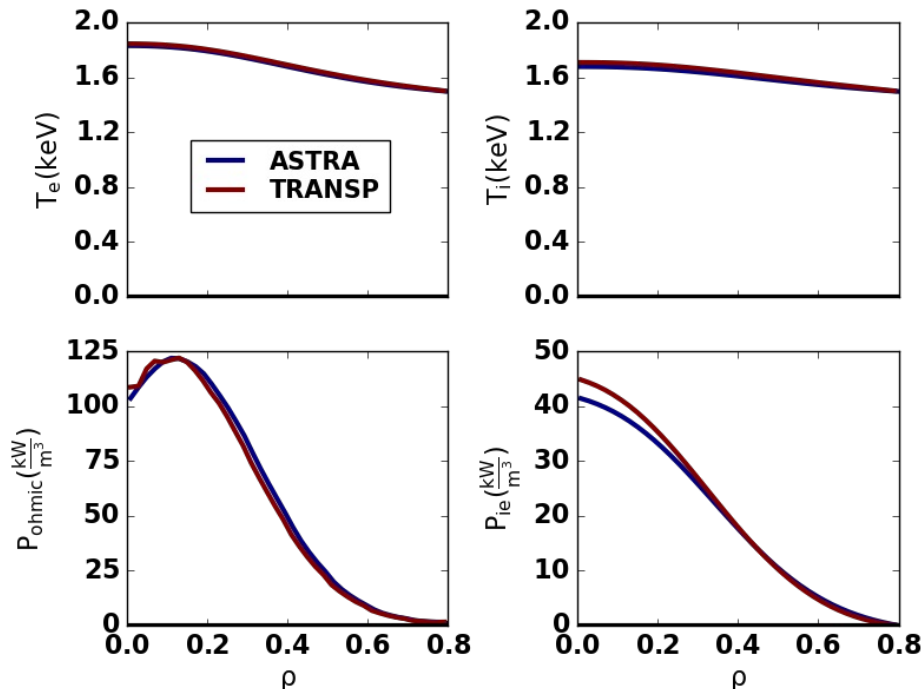


Integrated modeling verification: TRANSP and ASTRA yield different answers for realistic discharges

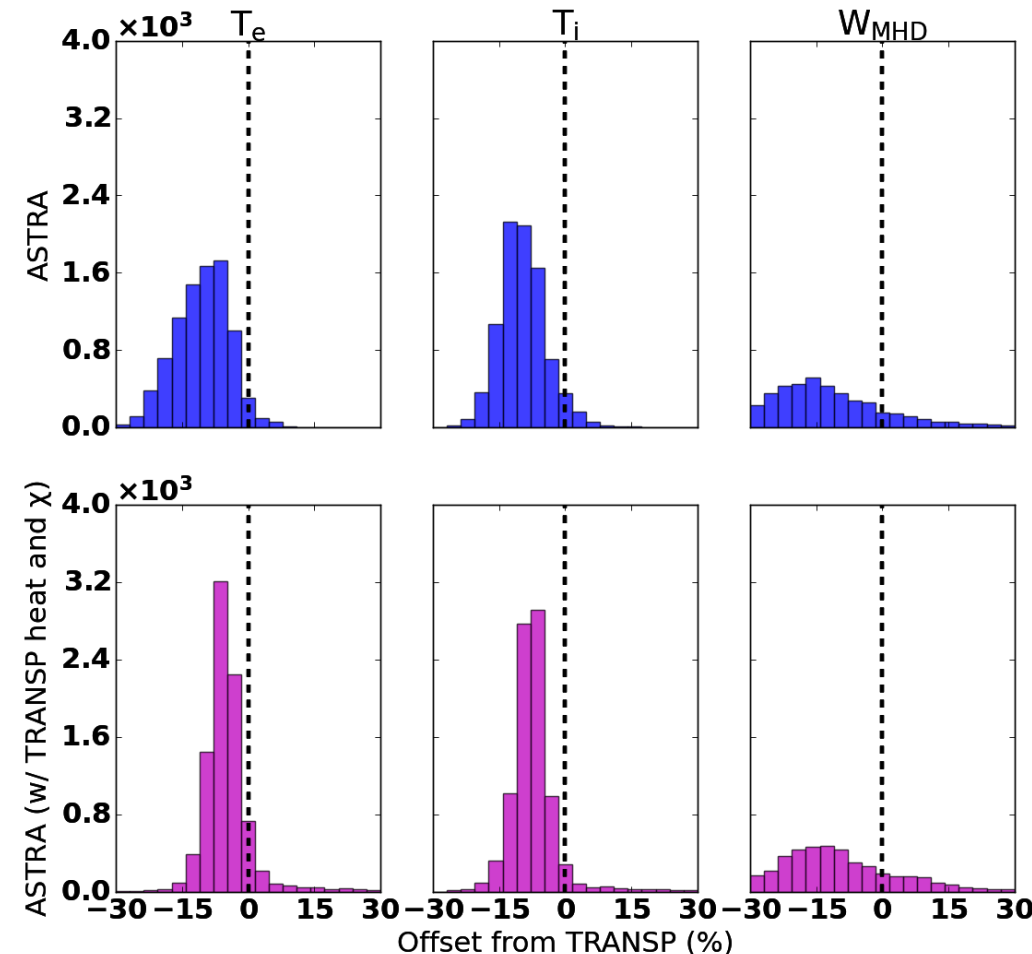
(ITER Physics Expert Group on Confinement and Transport, 1999)

- Verify predictions of core Te/Ti and Wmhd
- Simple case: ASTRA and TRANSP yield same result
- Database comparison: ASTRA and TRANSP differ
 - seemingly the solver?

Bias $\longrightarrow f = \frac{\langle T_{prediction} - T_{truth} \rangle}{\langle T_{truth} \rangle_{RMS}}$



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Integrated modeling validation: simple baselines of comparison

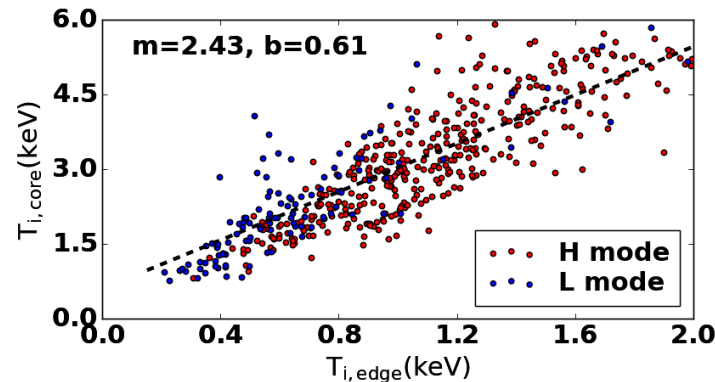
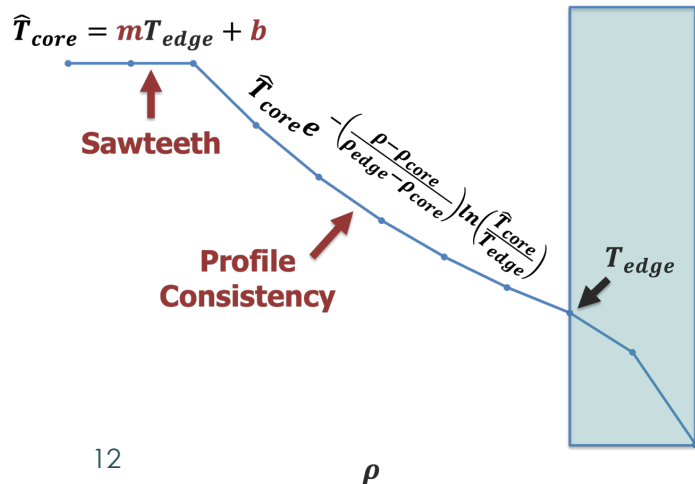
- **Validate predictions of core Te/Ti and Wmhd**
 - Use multiple independent transport solvers (TRANSP + ASTRA)
 - Run on ~hundreds of cases automatically
- **Compare to empirical baselines:**

Bias $\rightarrow f = \frac{\langle T_{prediction} - T_{truth} \rangle}{\langle T_{truth} \rangle_{RMS}}$

Error $\rightarrow \sigma = \frac{\langle |T_{prediction} - T_{truth}| \rangle_{RMS}}{\langle T_{truth} \rangle_{RMS}}$

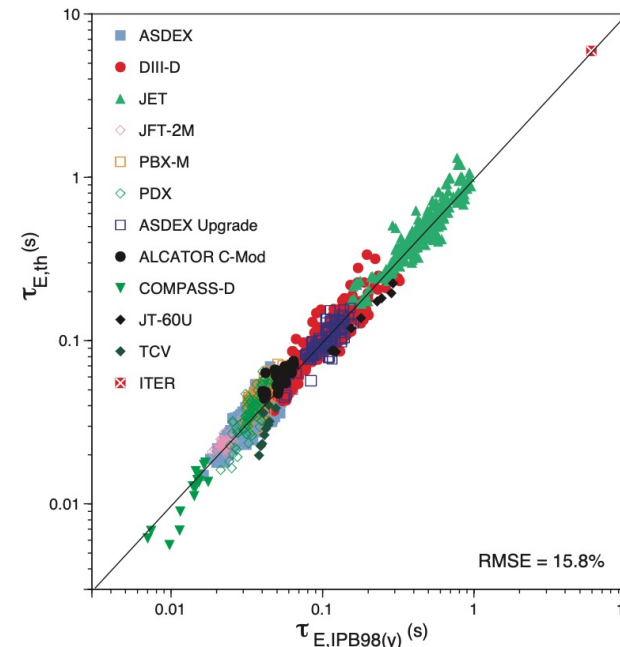
(ITER Physics Expert Group on Confinement and Transport, 1999)

Te/Ti baseline: “Profile consistency”



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Wmhd baseline: “H scaling”

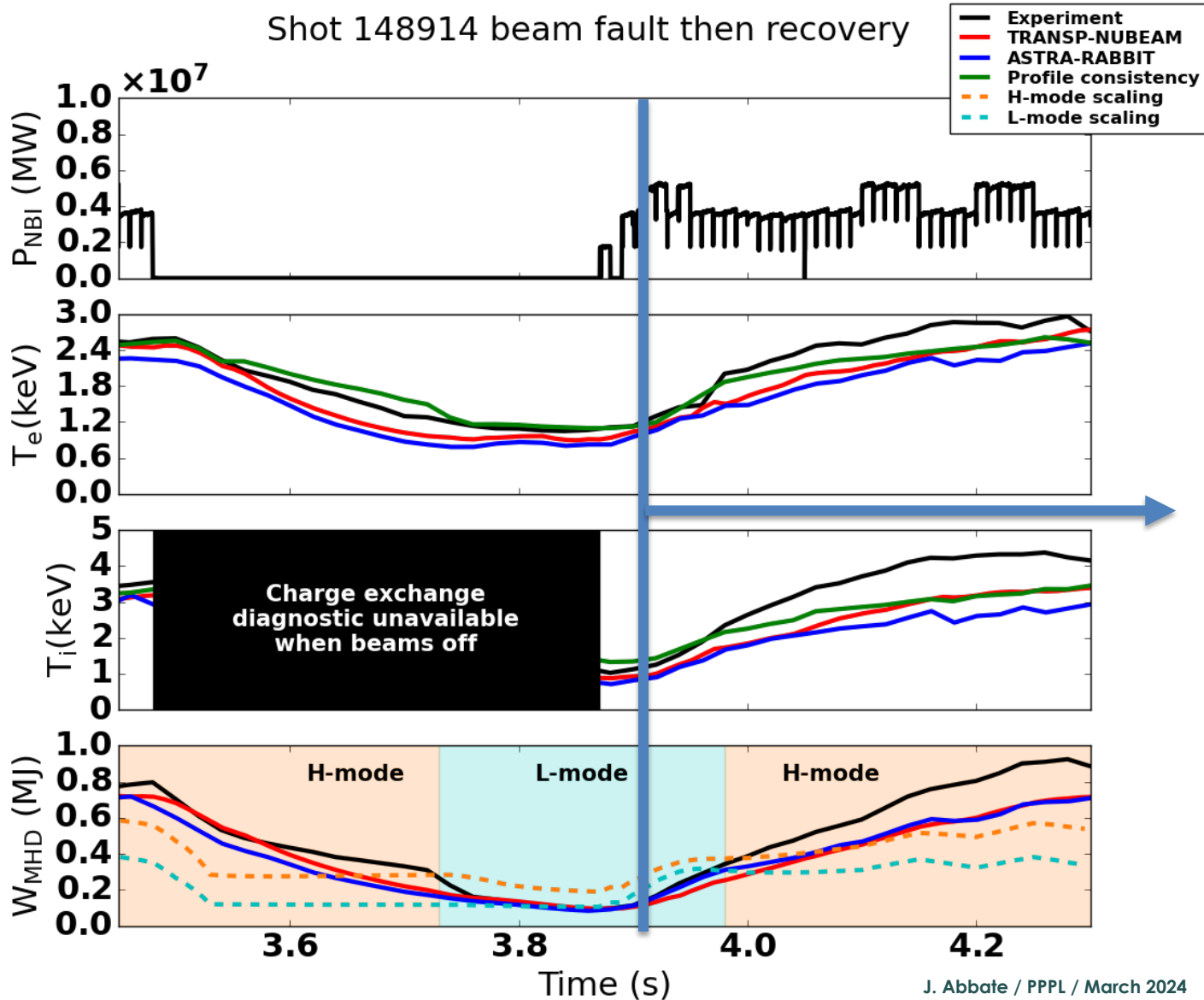


$$W_{MHD} = \tau_E P_{total}$$

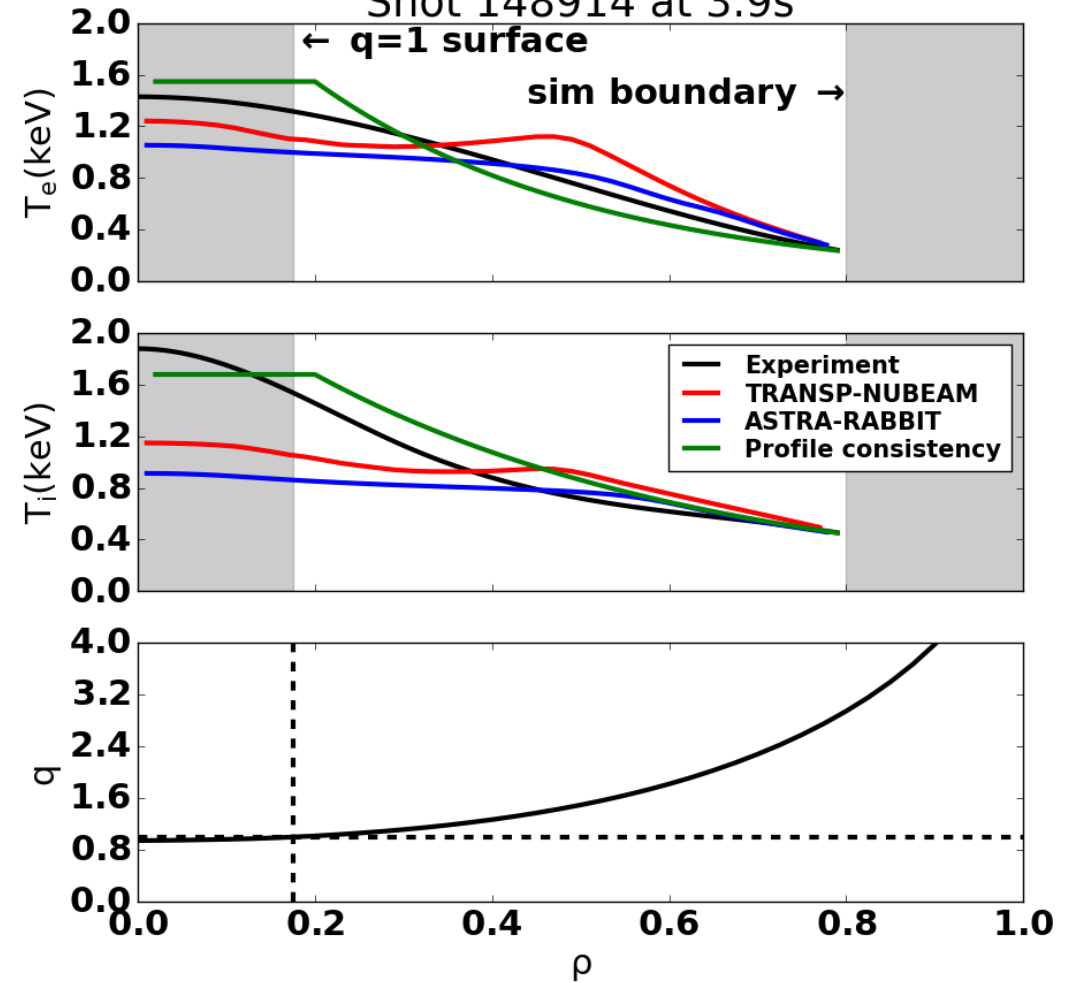


Time-dependent predictions made over 900ms window

Shot 148914 beam fault then recovery

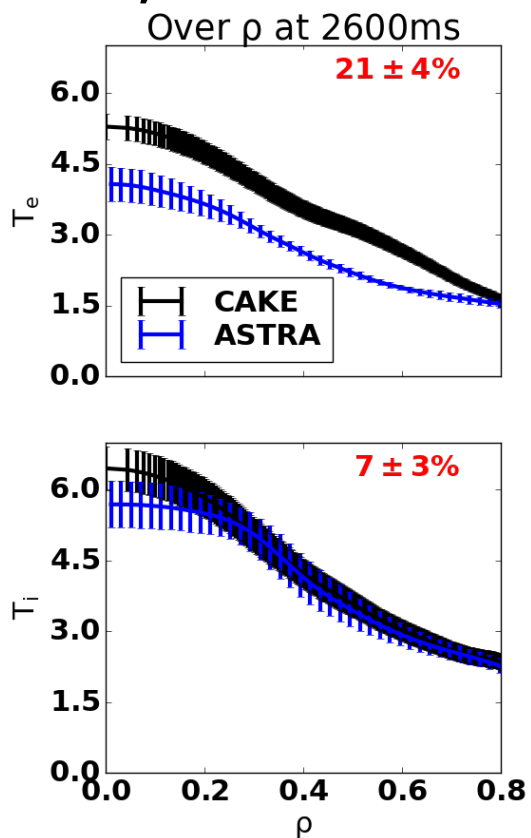


Shot 148914 at 3.9s

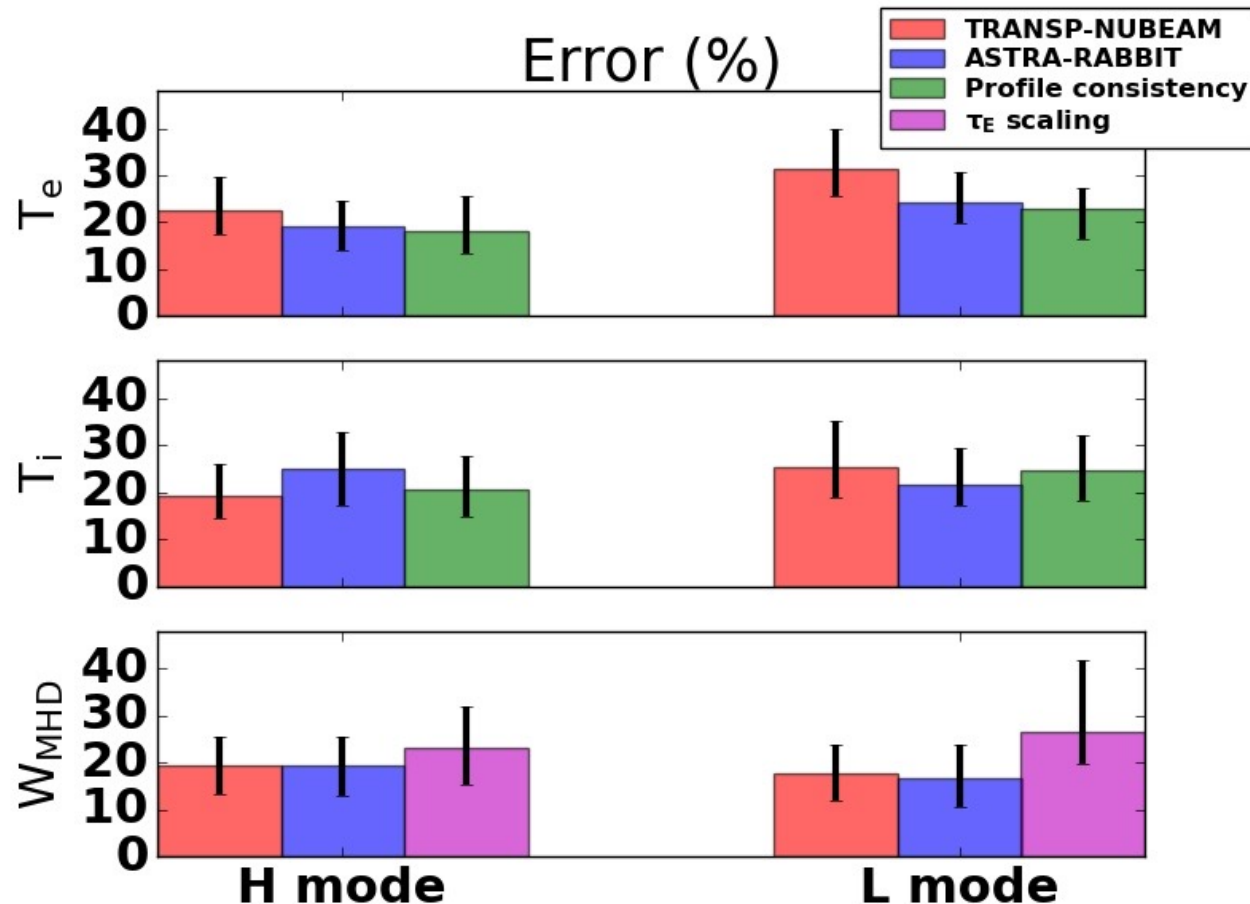


ASTRA/TRANSP perform no better than empirical baseline, large database with relatively low diagnostic uncertainty propagation gives confidence

- **Hypothesis: ASTRA/TRANSP performs significantly better than baseline**
 - $p < 0.05$ for W_{mhd} but not T_e/T_i
- **Diagnostic uncertainty $\lesssim 5\%$ for single shot; less for mean over database**



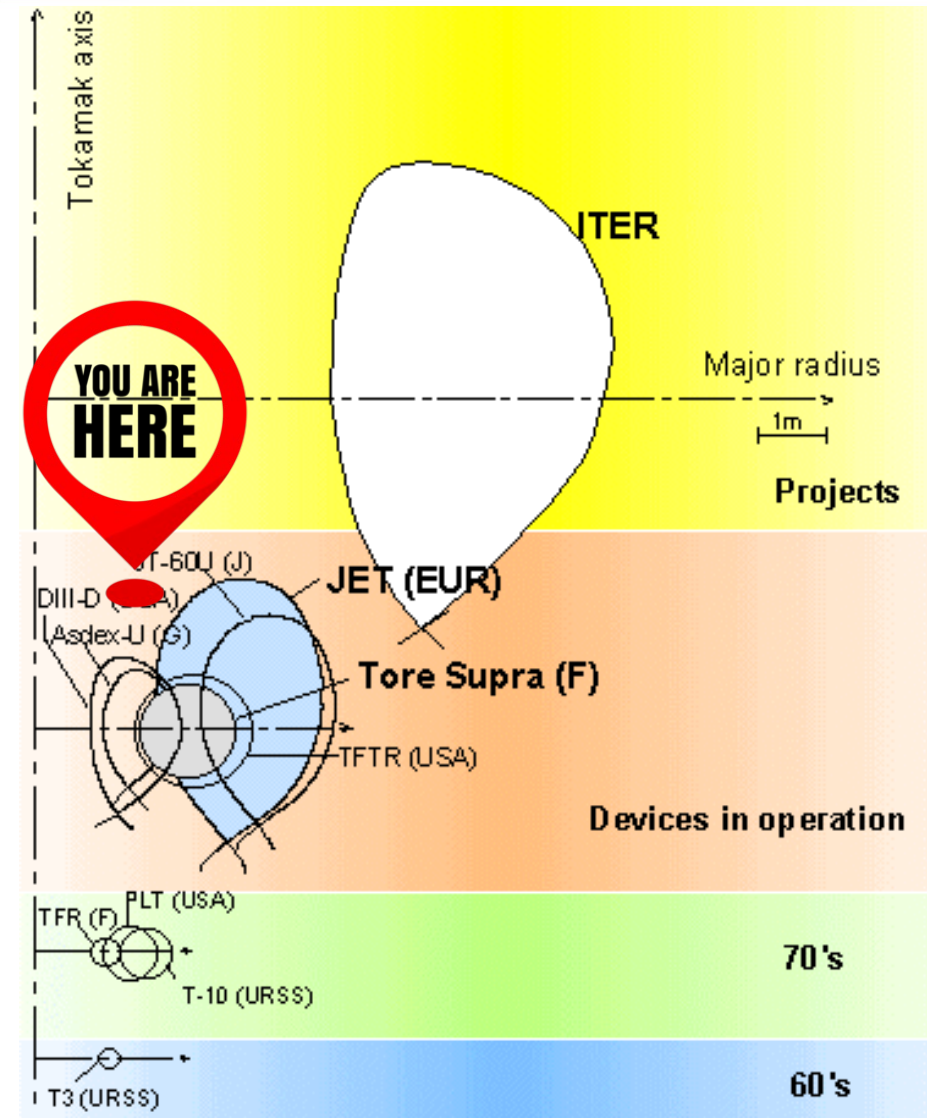
	Input	Output
T_e	6%	4%
T_i	9%	3%
n_e	6%	3%
Z_{eff}	5%	1%
Ω	9%	1%
q	10%	4%



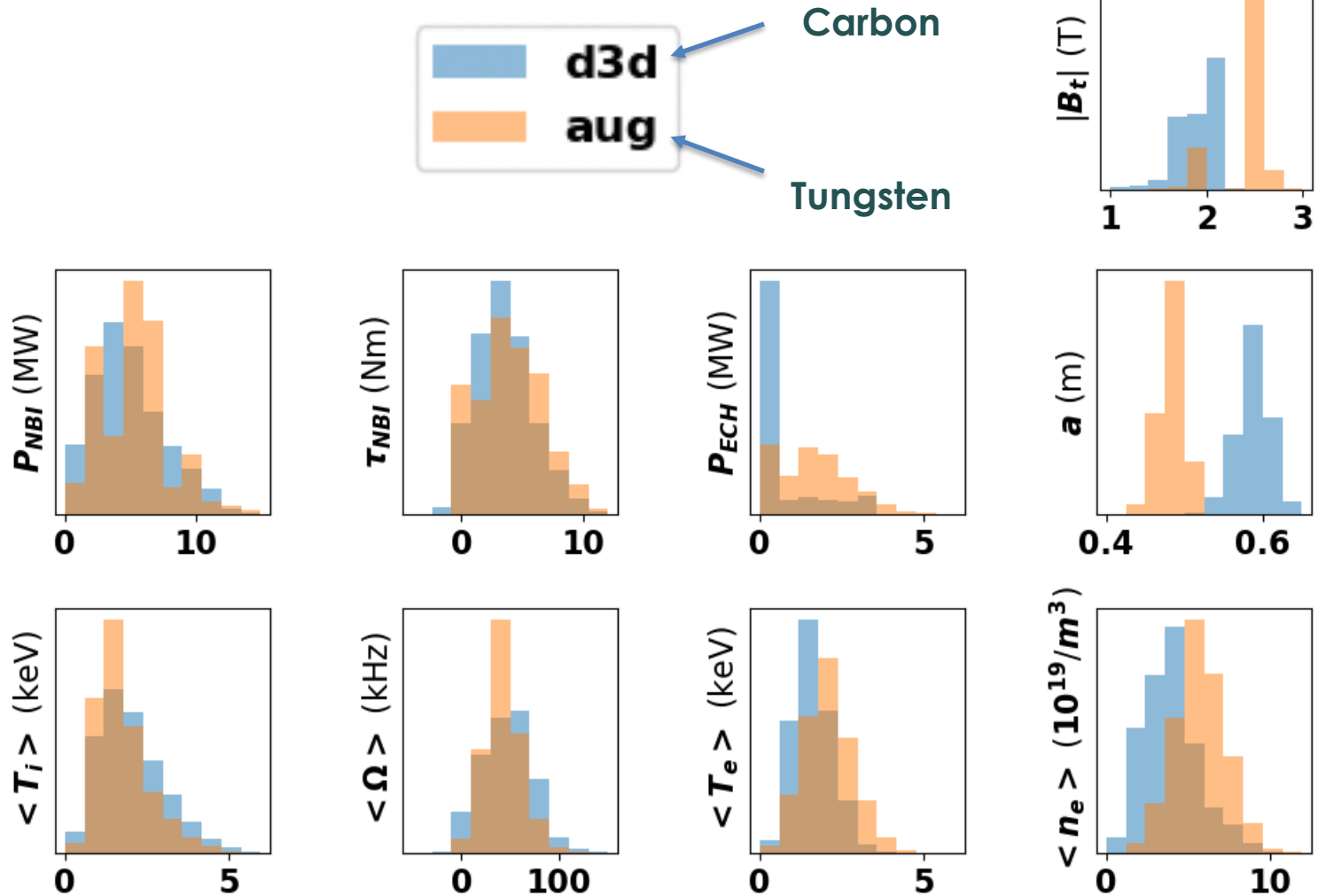
Training a model for the task of extrapolation: 4 methods for data+sim (one of which was already successful)

- **Reactor commissioning: use *all* information until current timestep to predict future evolution**
 - All timesteps / discharges up to now
 - Simulations
 - Previous tokamaks
 - **Our emulation: Train on D3D $I_p < 0.9$ MA, predict on D3D $1.0 \text{ MA} < I_p < 1.2 \text{ MA}$**
 - Add AUG data
 - Add ASTRA simulation info
-
- ✗ **1. Add data from more machines using normalization**
 - ✗ **2. Concatenate simulation context as additional input**
 - ✗ **3. Transfer learn by training on experimental data, tuning on simulation data**
 - ✓ **4. Meta-learned model taking output of data-driven and simulation *models***

Add data from more machines: AUG data to enhance D3D predictions



The main tokamaks in the world,
French Atomic Energy Commission (CEA)



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Hypothesize normalization aids cross-machine learning

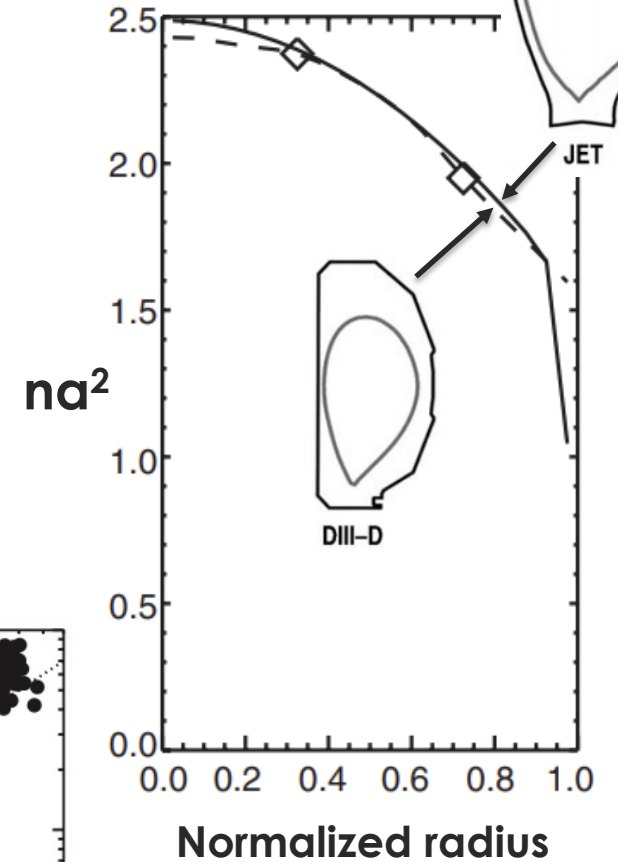
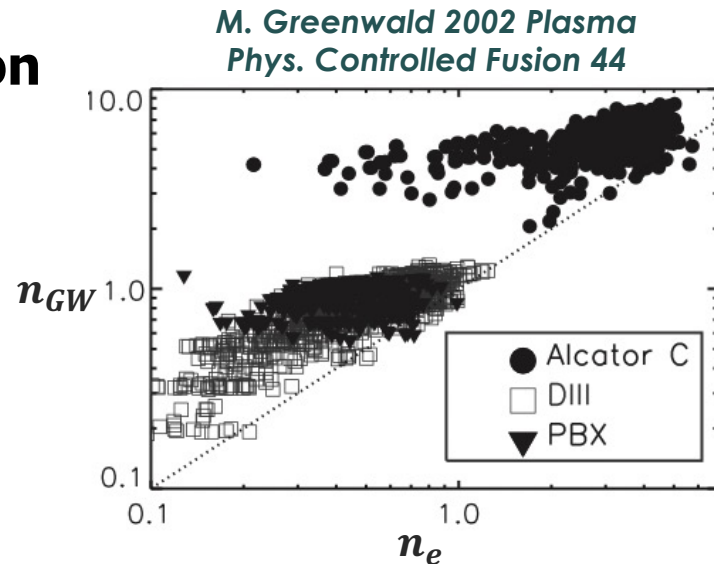
- **Physics: nondimensionalizing Vlasov eq**
 - **BUT no quantitative accuracy in most cases** (atomic physics, 3D fields, boundary effects...)
- **Physics (simple):**

$$\Omega \rightarrow R^2 \Omega \int n_e dV$$

$$P \rightarrow \frac{P}{V}$$

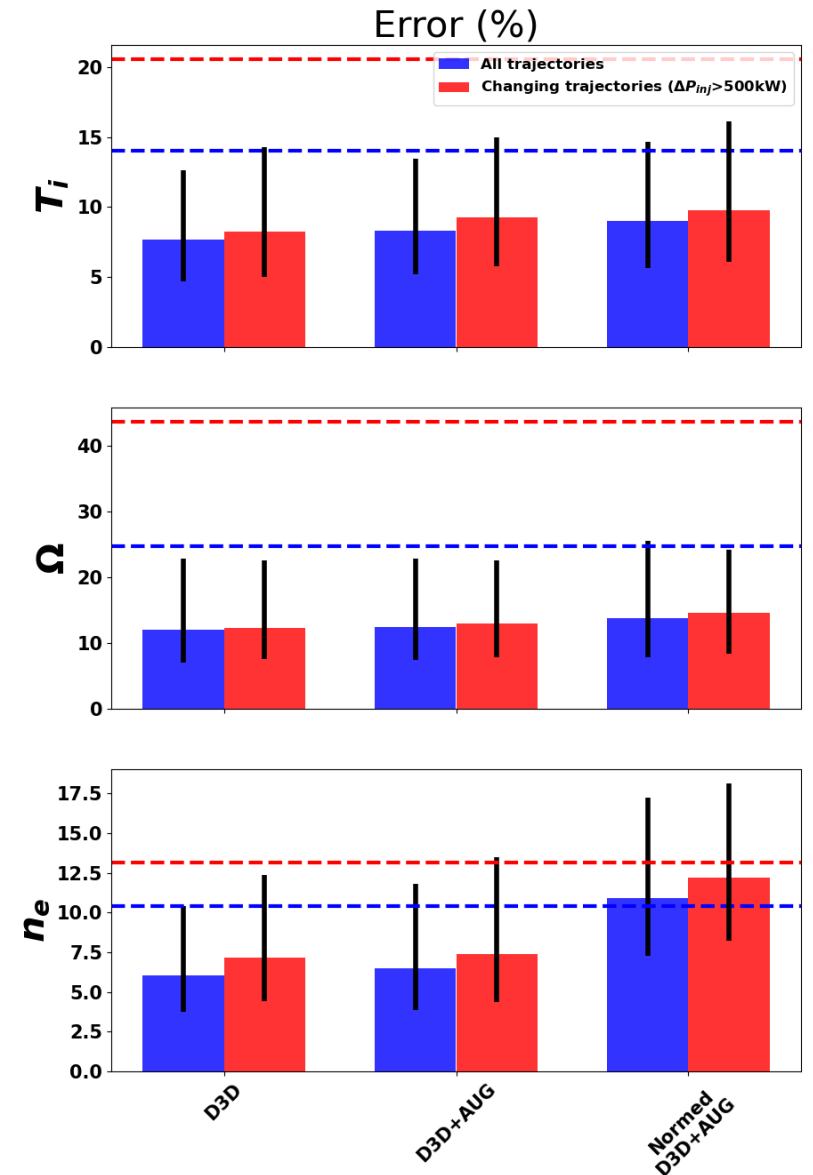
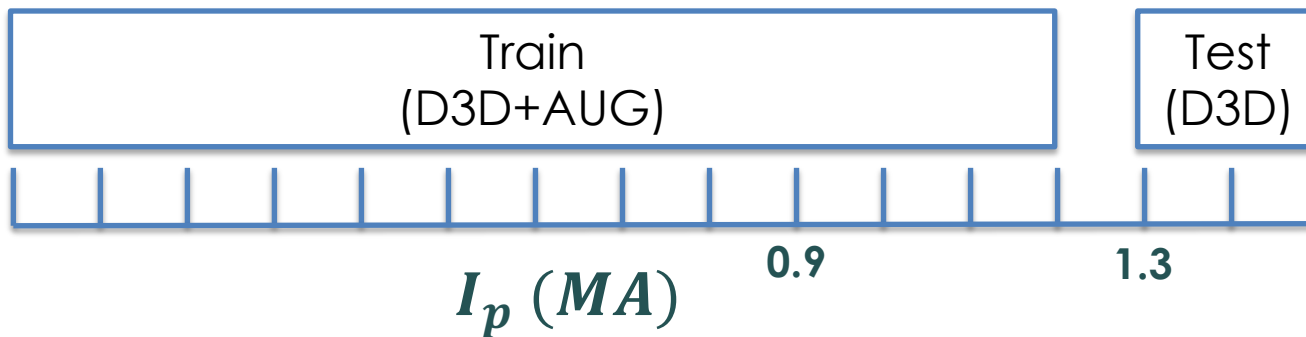
- **Empirical: operators observe degradation** as density approaches $n_{GW} = \frac{I_p}{\pi a^2}$

$$n_e \rightarrow \frac{n_e}{n_{GW}}$$

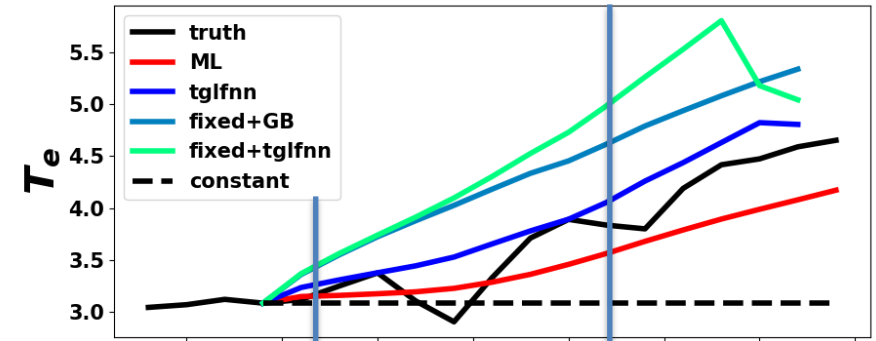
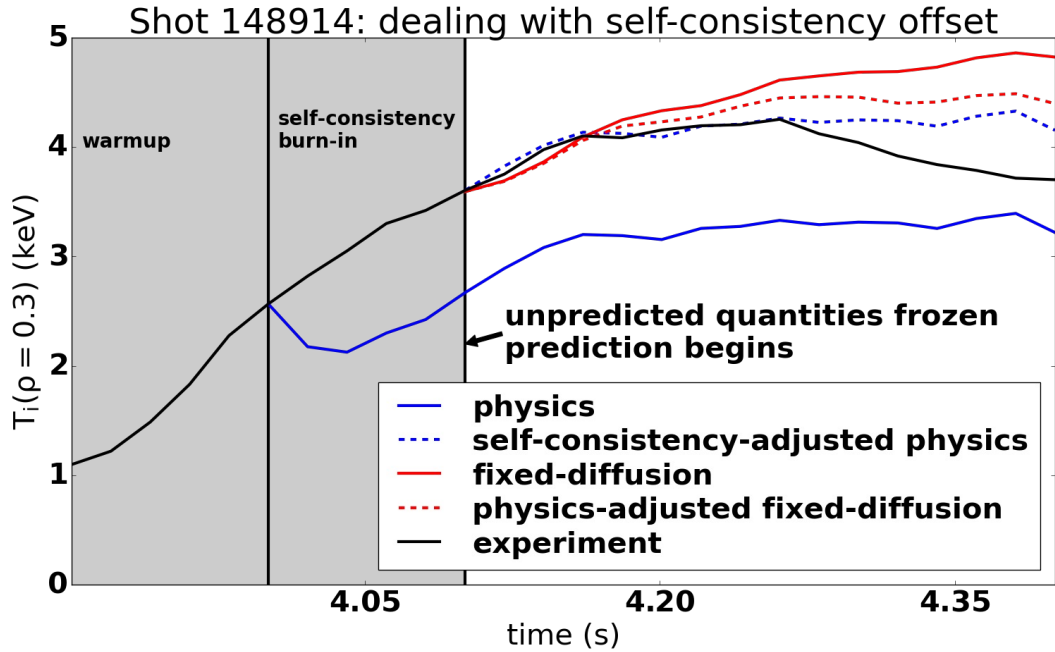


Add data from more machines: does not improve performance

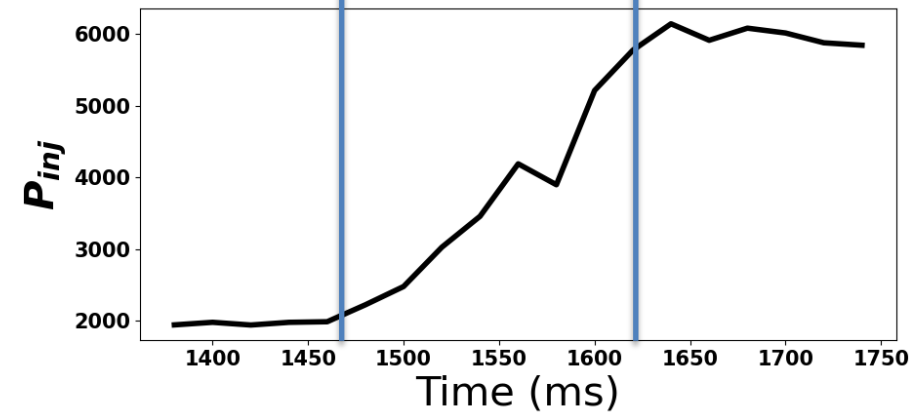
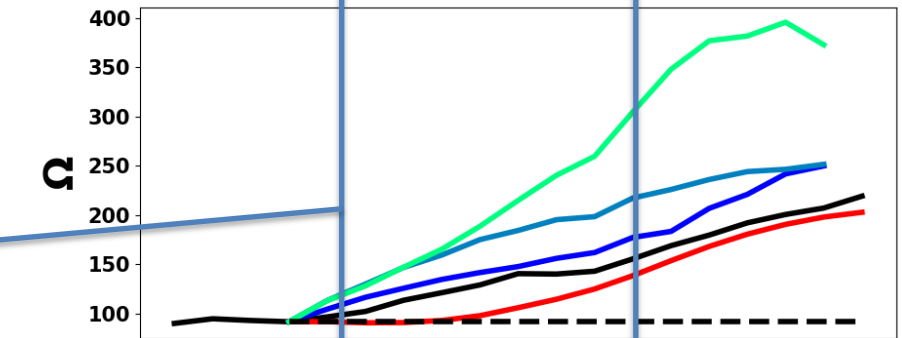
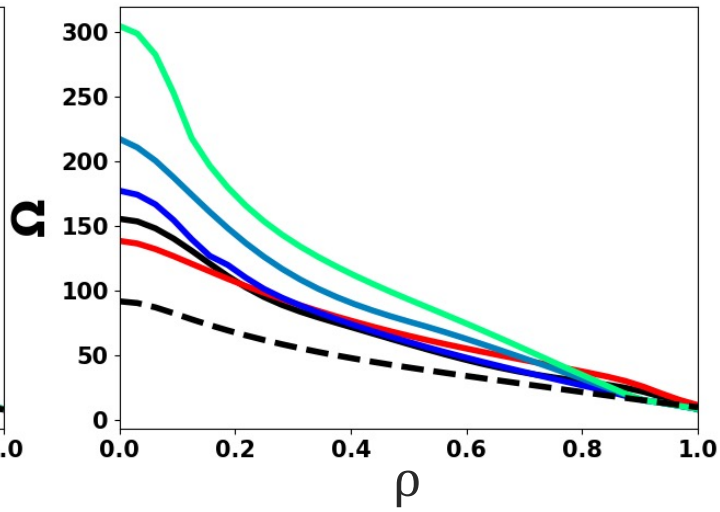
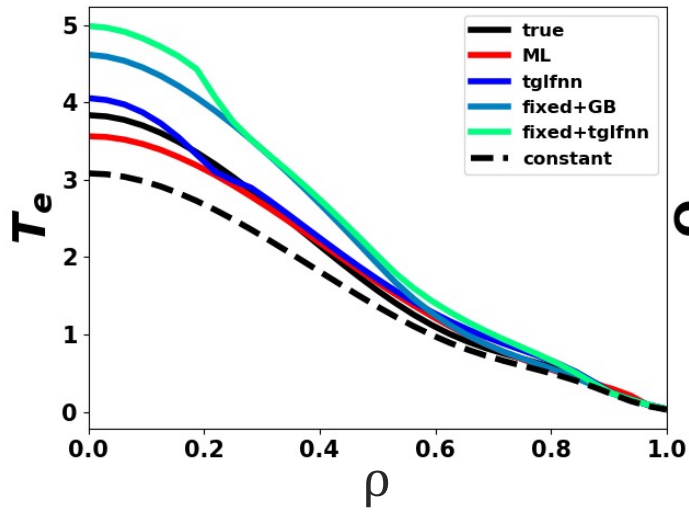
- **Consider ITER commissioning: using data up to now, predict next shot**
 - No improvement from including AUG data
- “Constant prediction” for reference
- **Time-dependent vs steady-state trajectories**
 - Based on $\Delta P_{inj} > 500\text{kW}$
- **UPSHOT: don't skimp on ITER pre-operation phase**
 - Maybe more machines helps learn own normalization?



The ensemble of simulators

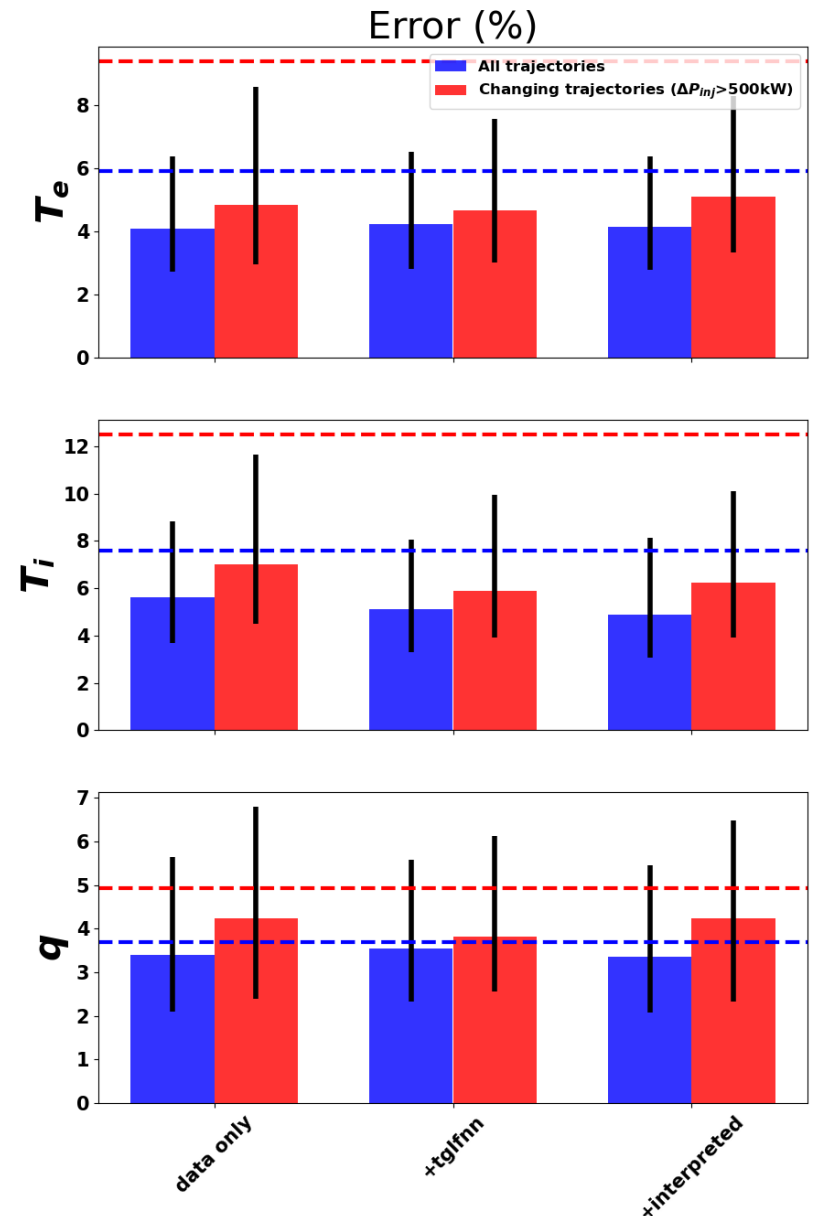
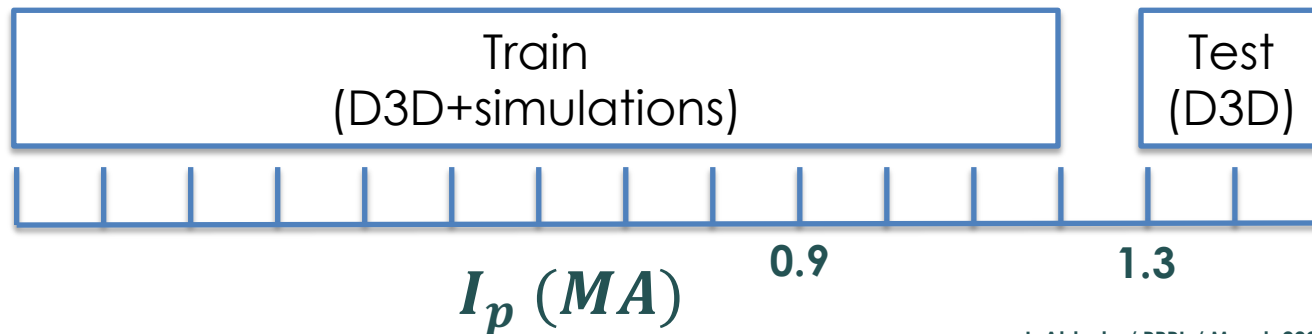


Shot 189510 1460-1620ms



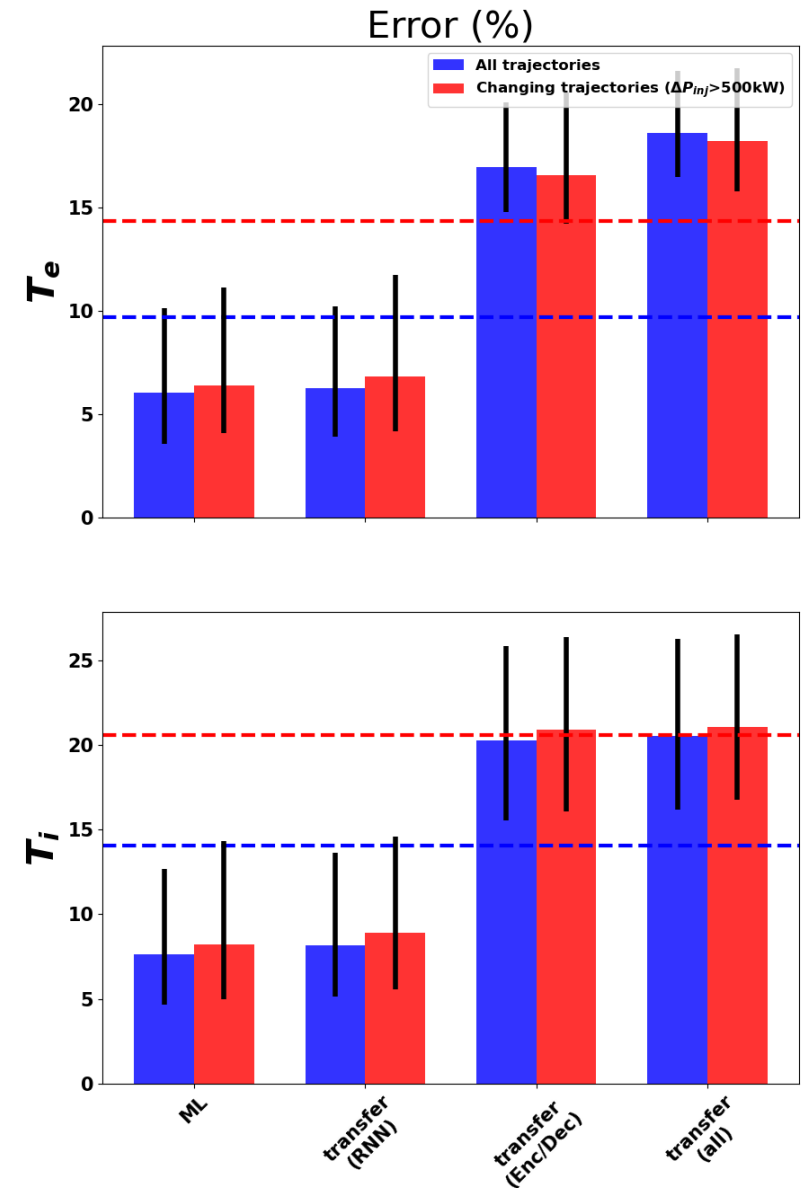
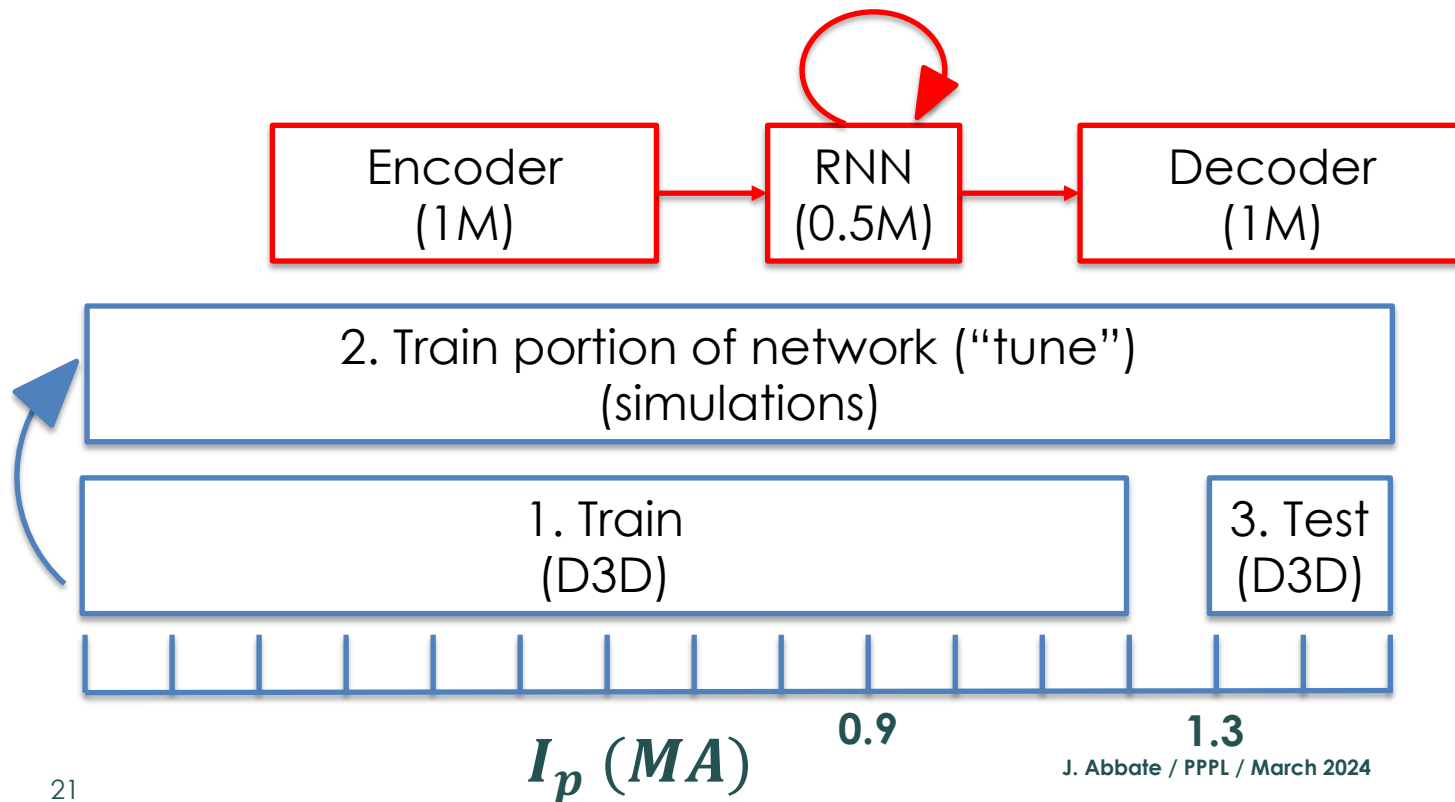
Concatenate simulation context as additional input

- **Predicted quantities**
 - Core electron, ion temperature (TGLF-nn)
- **Interpreted quantities**
 - Total heat to electrons, ions
 - Driven current
- **No statistically significant improvement over data-driven model for any signal**
- **UPSHOT: details of heat and current deposition do not seem important (\sim profile consistency)**
 - Maybe more / better simulations?



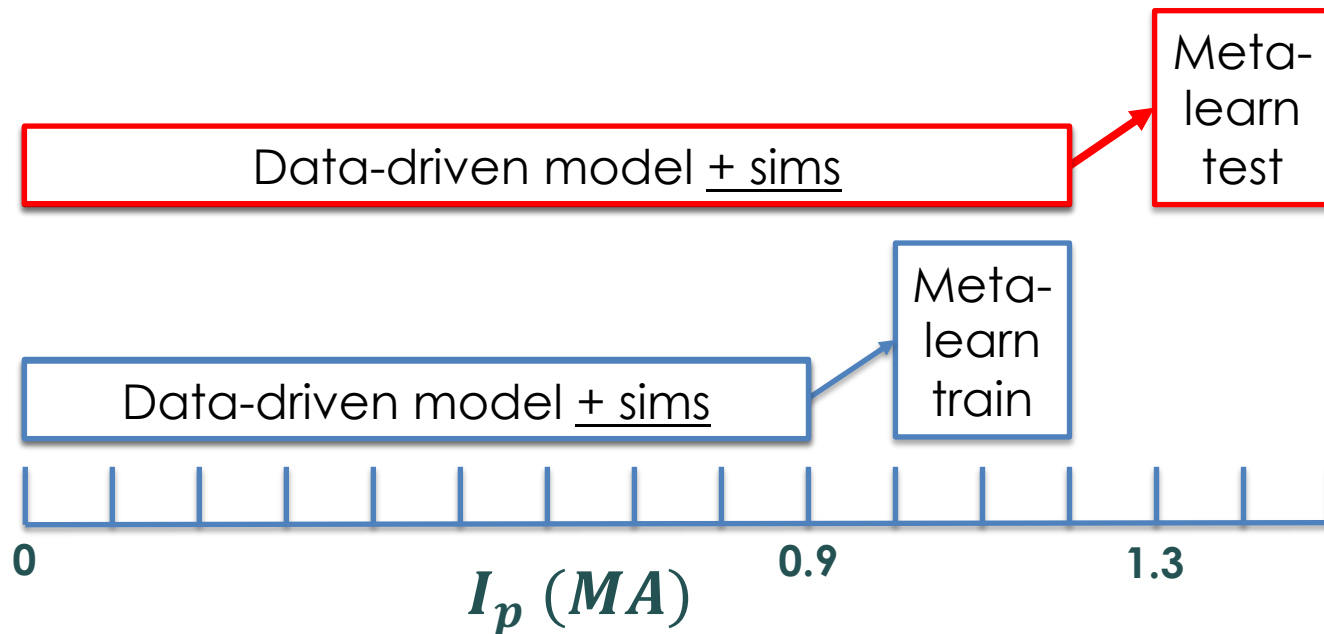
Transfer learn by training on experiment data, tuning on simulation

- Pretend simulations are reality in regimes we haven't yet seen
- Once again: no significant improvement
- UPSHOT: simulations are not quantitatively accurate
 - Again, maybe more/better simulations?

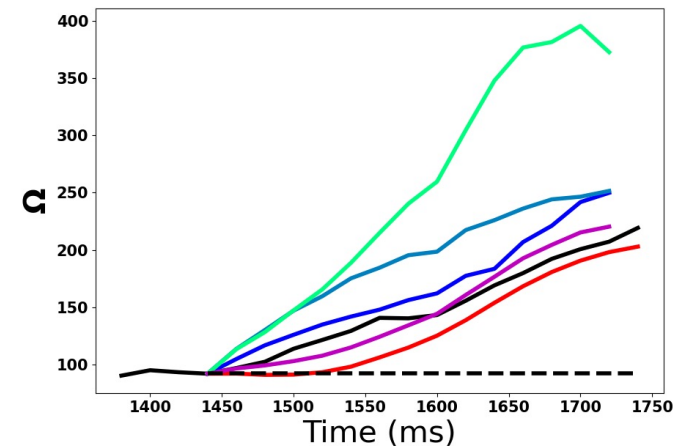
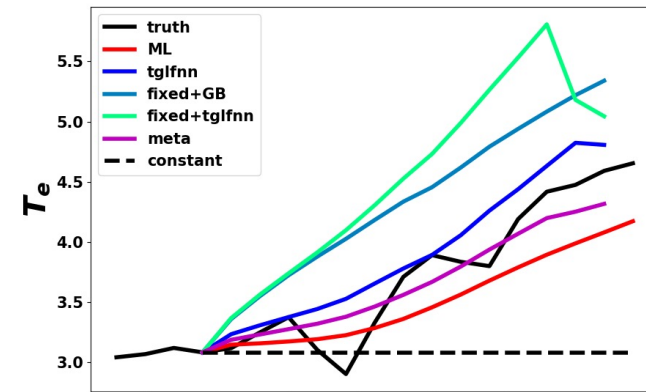


Meta-learned model ensembling output of data-driven and physics models

- **Explicitly train model for *task* of extrapolation**
- **Train data-driven model(s) on one dataset**
- **Build meta-learning model that predicts on extrapolated dataset given model output**
- **Also consider simulations on equal footing**

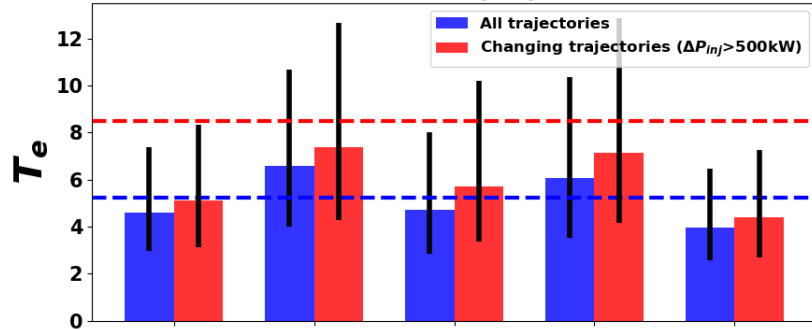


E.g. logistic regression: learn coefficients in T_{meta}

$$= \alpha_{data} T_{data} + \alpha_{TGLFnn} T_{TGLFnn} + \alpha_{fixedGB} T_{fixedGB} + \alpha_{fixedTGLFnn} T_{fixedTGLFnn}$$


Meta-learned model outperforms data-driven or simulations alone!

Error (%)



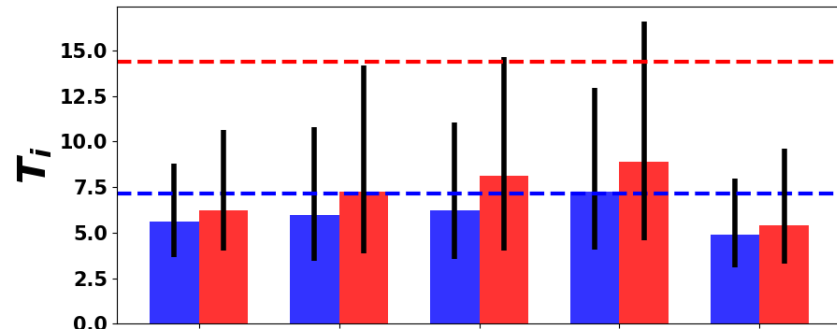
$$\alpha_{data} = 64\%$$

$$\alpha_{fixedGB} = 19\%$$

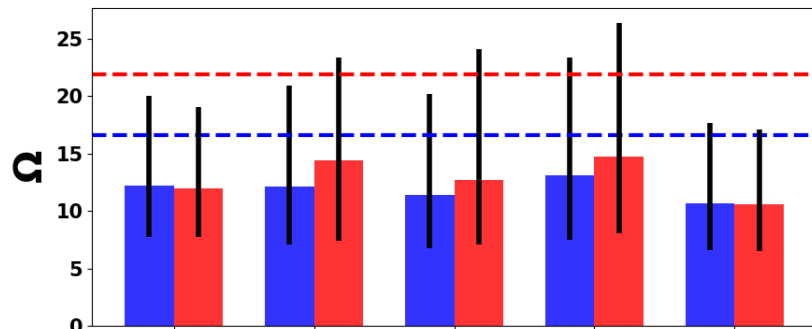
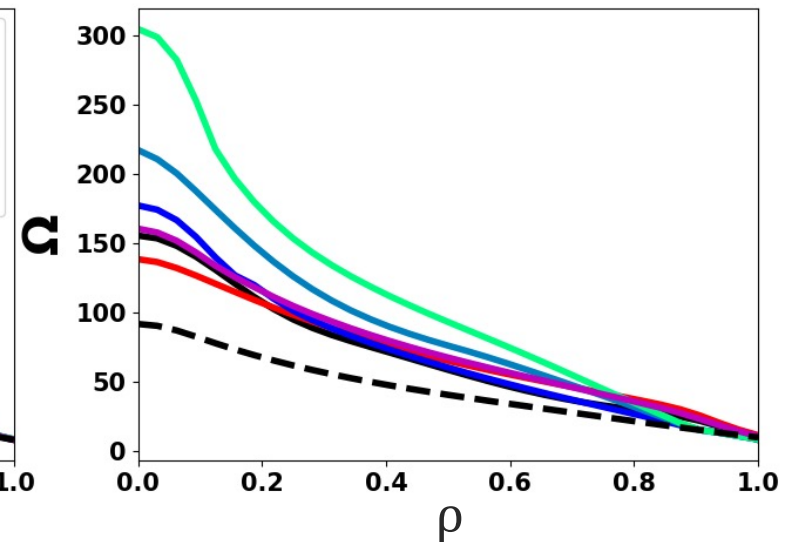
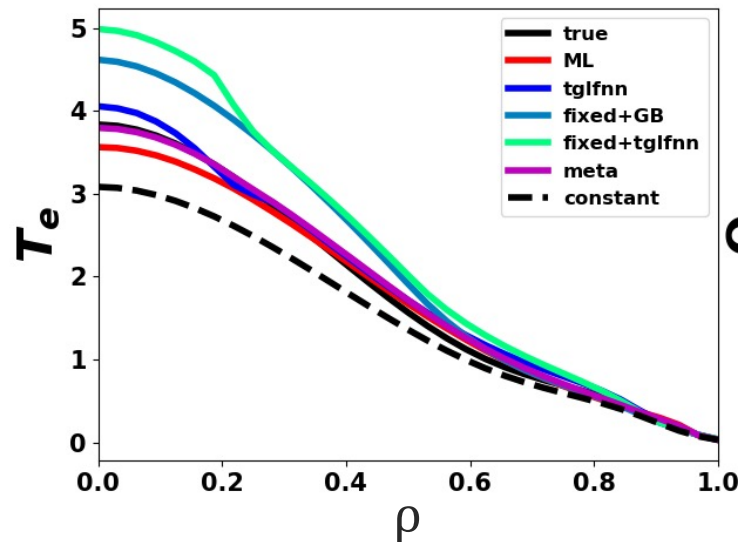
$$\alpha_{TGLFnn} = 15\%$$

$$\alpha_{fixedTGLFnn} = 2\%$$

E.g. logistic regression: learn coefficients in T_{meta}

$$= \alpha_{data} T_{data} + \alpha_{TGLFnn} T_{TGLFnn} + \alpha_{fixedGB} T_{fixedGB} + \alpha_{fixedTGLFnn} T_{fixedTGLFnn}$$


Shot 189510 1460-1620ms



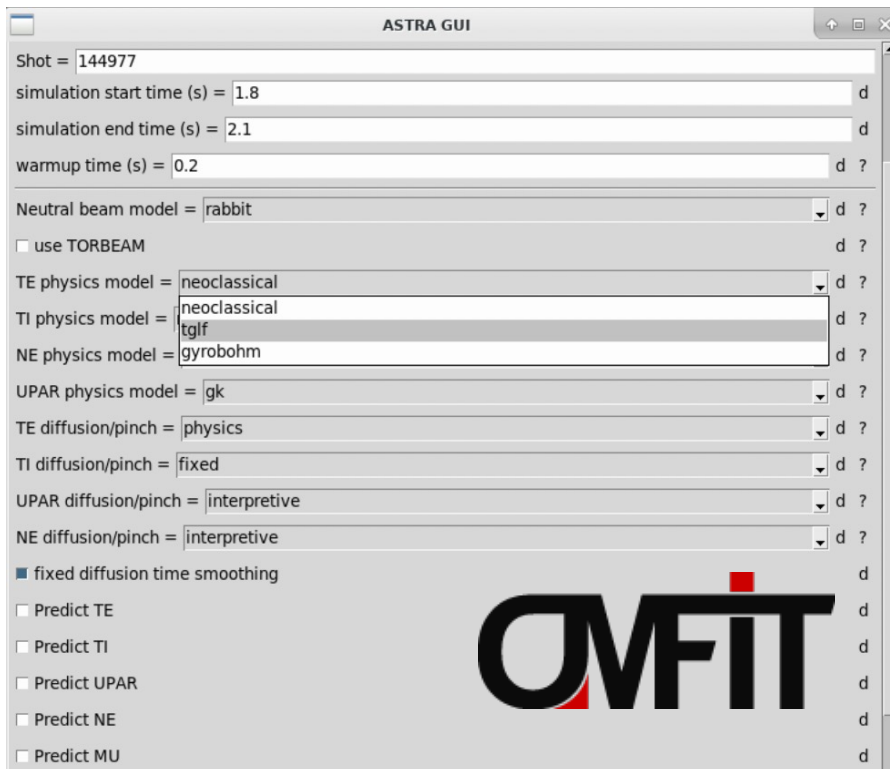
Thesis contributions: guidance

- **“Always have a baseline”**: use hypothesis testing for validation
- **Database scans are useful (less bias, more confidence)**
- **Simple simulation context doesn’t aid predictions**
 - **Like profile consistency: details of heat deposition don’t matter**
- **ITER will need to rely largely on its own data for control development**
 - **Don’t sacrifice pre-operation commissioning time for sake of speed**
- **Take a clear stance on spectrum of “end-to-end” to “interpretable” models**
 - **Setting low-level vs high-level control targets (e.g. gas vs target density)**
 - **Predicting diagnostics directly vs fitted profiles**
- **Once we have a clear task to deploy, an open competition would be effective**
 - **If data access a problem, then at least within the fusion community**

Thesis contributions: infrastructure

- **With Emiliano/Giovanni, upgraded ASTRA and made OMFIT interface**
- **Pipeline for fetching standardized dataset (feat. Brian Sammuli's toksearch)**
- **With Rory, neural network control in DIII-D PCS**
- **With Ian, arbitrary-timestep profile dynamics models**
- **With Viraj/Allen/Andy/Ian, Chat-D3D**

tinyurl.com/abbate-phd-defense

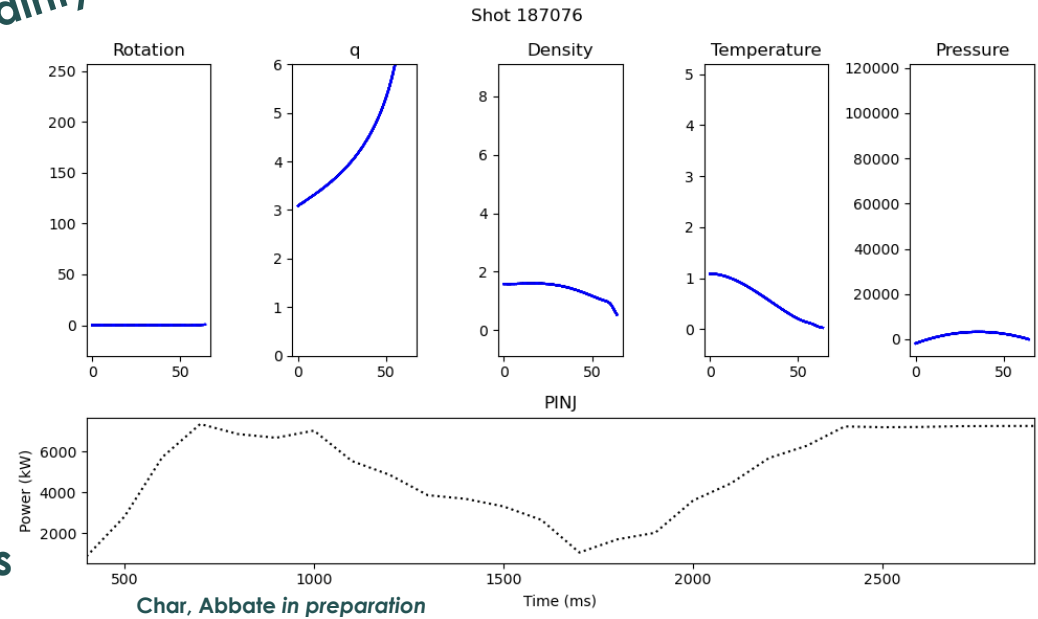
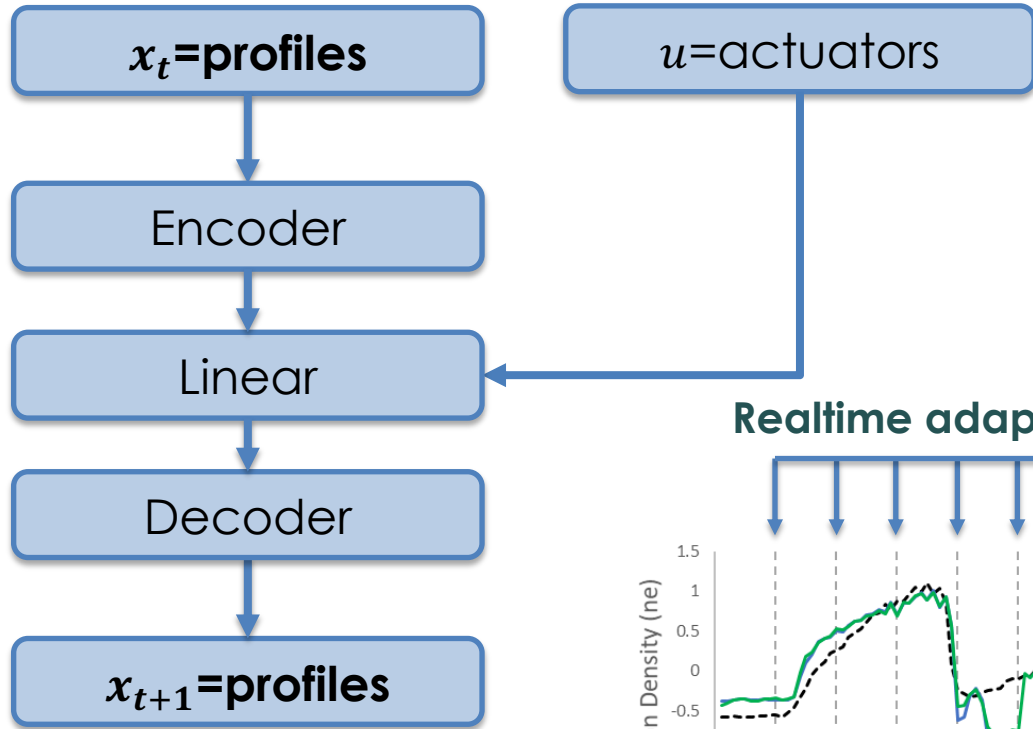


The image shows a screenshot of a chat conversation on Chat-DIII-D. The chat is titled "Chat-DIII-D BOT" and is dated "Today at 5:12 PM". The user "Viraj Mehta" asks: "how can we control Alfvén eigenmodes? please reference specific shots in your answer". The chat bot responds: "To control Alfvén eigenmodes (AEs), several experimental approaches have been used in previous DIII-D shots. One approach is to use localized electron cyclotron heating (ECH) to alter the beam-driven AE activity. Shots 128564, 128560, and 128562 from mini-proposal 2007-21-10 investigated this method. In shot 128564, ECH power was deposited near q_{min} , resulting in a dramatic reduction or suppression of RSAEs. The localized ECH had a significant impact on the AE activity, indicating the potential for AE control using ECH. Another approach is to use neutral beam injection (NBI) power and voltage variations as actuators. Shots 163146, 163175, and 154102 from mini-proposal 2017-24-89 explored this method. In shot 163146, a left beam power scan was performed to control AE activity. By decreasing the beam power, the amplitude of AEs was depressed. The reduction in AE activity was observed through real-time electron cyclotron emission (ECE) measurements. Shot 163175 tested the use of NBI voltage variation as an actuator to control reversed shear Alfvén eigenmodes (RSAEs). By decreasing the beam voltage, the RSAEs were further reduced, indicating the potential for voltage manipulation to control AE activity. In shot 154102, both on-axis and off-axis beams were used to scan NBI power during the current ramp. The objective was to determine the effect of off-axis injection on AE activity and fast ion transport. The shots provided valuable data on the stability and structure of AEs under different injection configurations. These examples highlight the potential for controlling AEs through localized ECH deposition and NBI power and voltage variations. By manipulating these parameters, the activity and amplitude of AEs can be effectively modified."

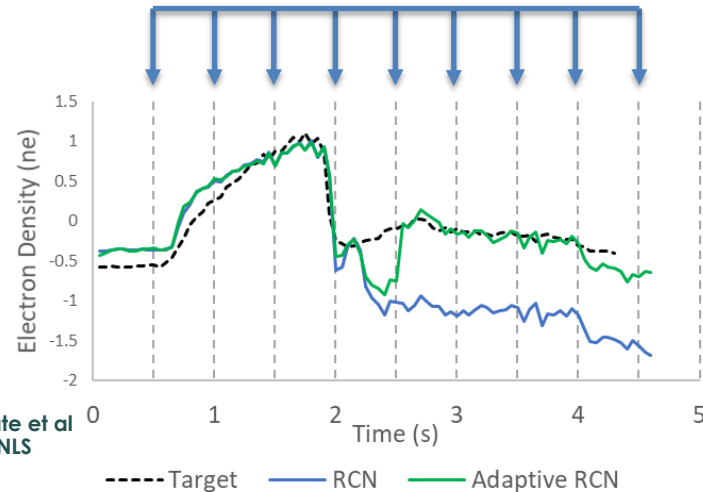


Work in progress: Upgrades for profile prediction

Linear-state-space model



Realtime adapt every 500ms



Jalalvand, Abbate et al
2022 IEEE TNNLS

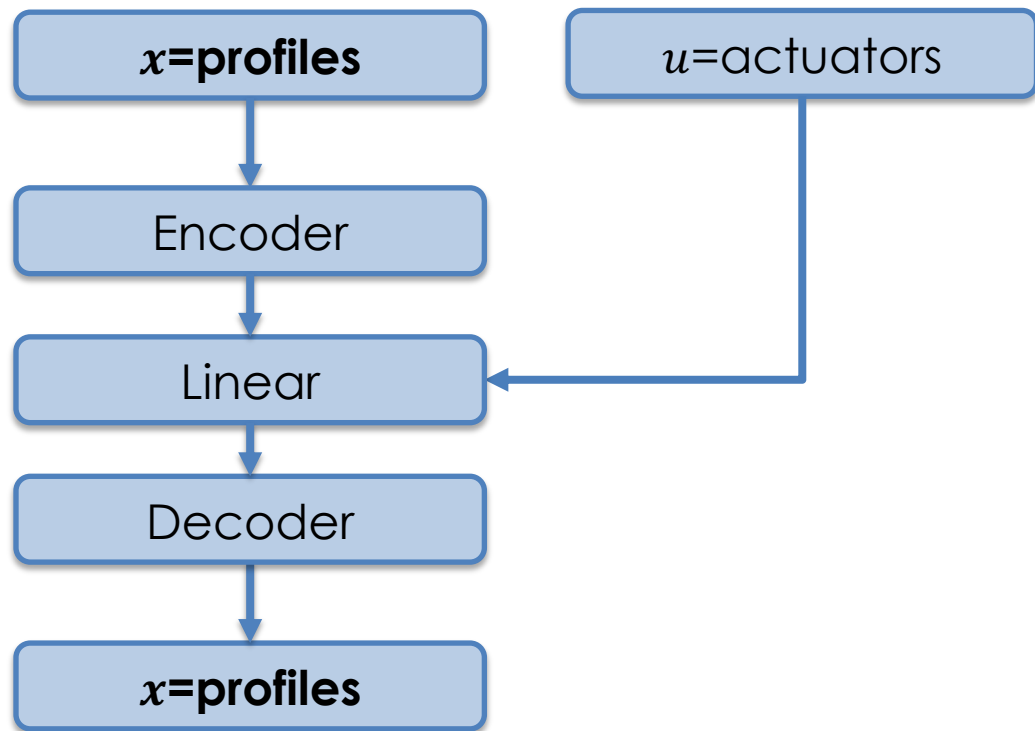
J. Abbate / PPPL / March 2024

Find mapping f s.t.
$$x_{t+1} = f(x_t, u_t, u_{t+1})$$



Backup slides

“Linear latent space” approach to leverage full Model-Predictive Control



$$z = f(x)$$

$$z_{t+1} = Az_t + Bu_t$$

$$z_{t+2} = Az_{t+1} + Bu_{t+1} = A^2z_t + ABu_t + Bu_{t+1}$$

...

$$z_{t+N} = A^N z_t + A^{N-1} Bu_t + \dots + Bu_{t+N}$$

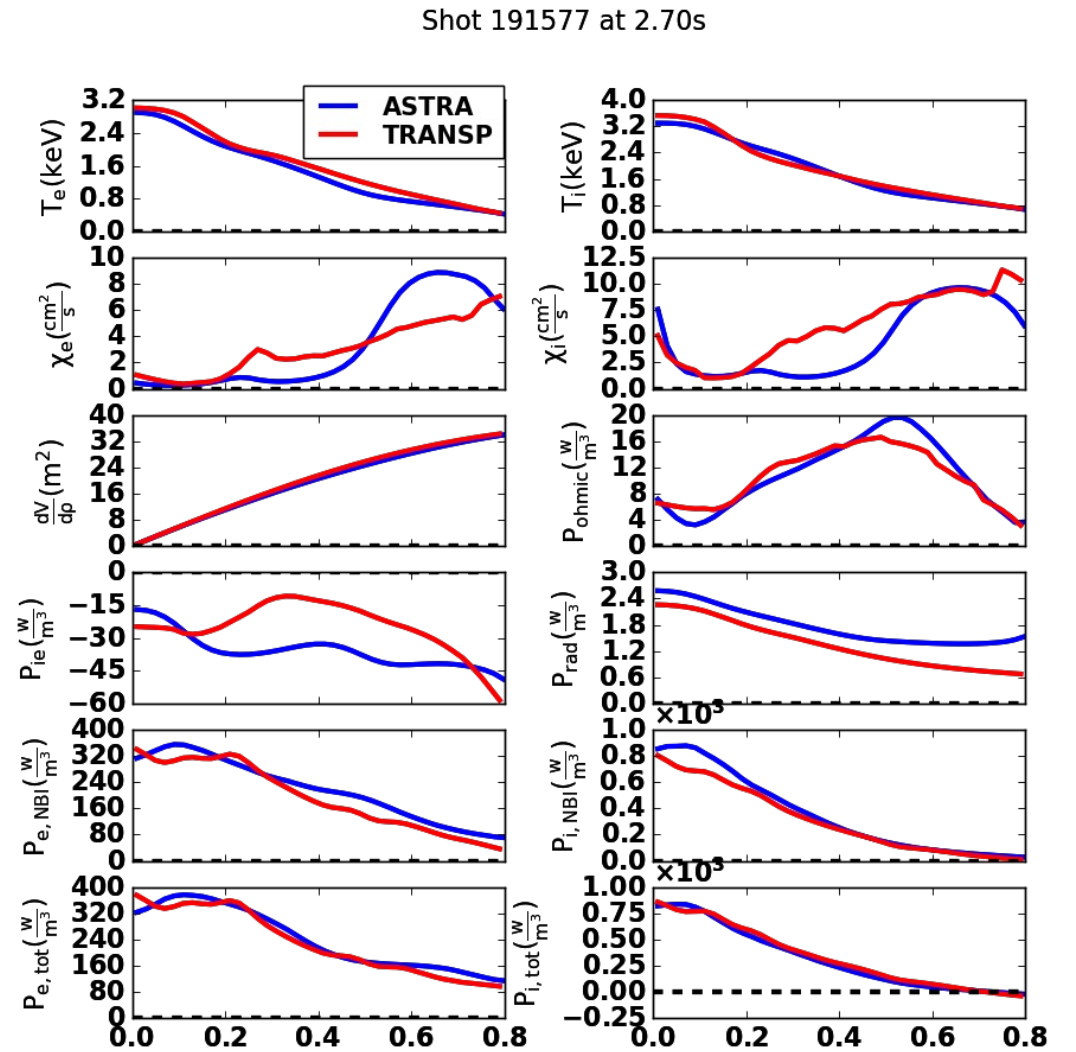
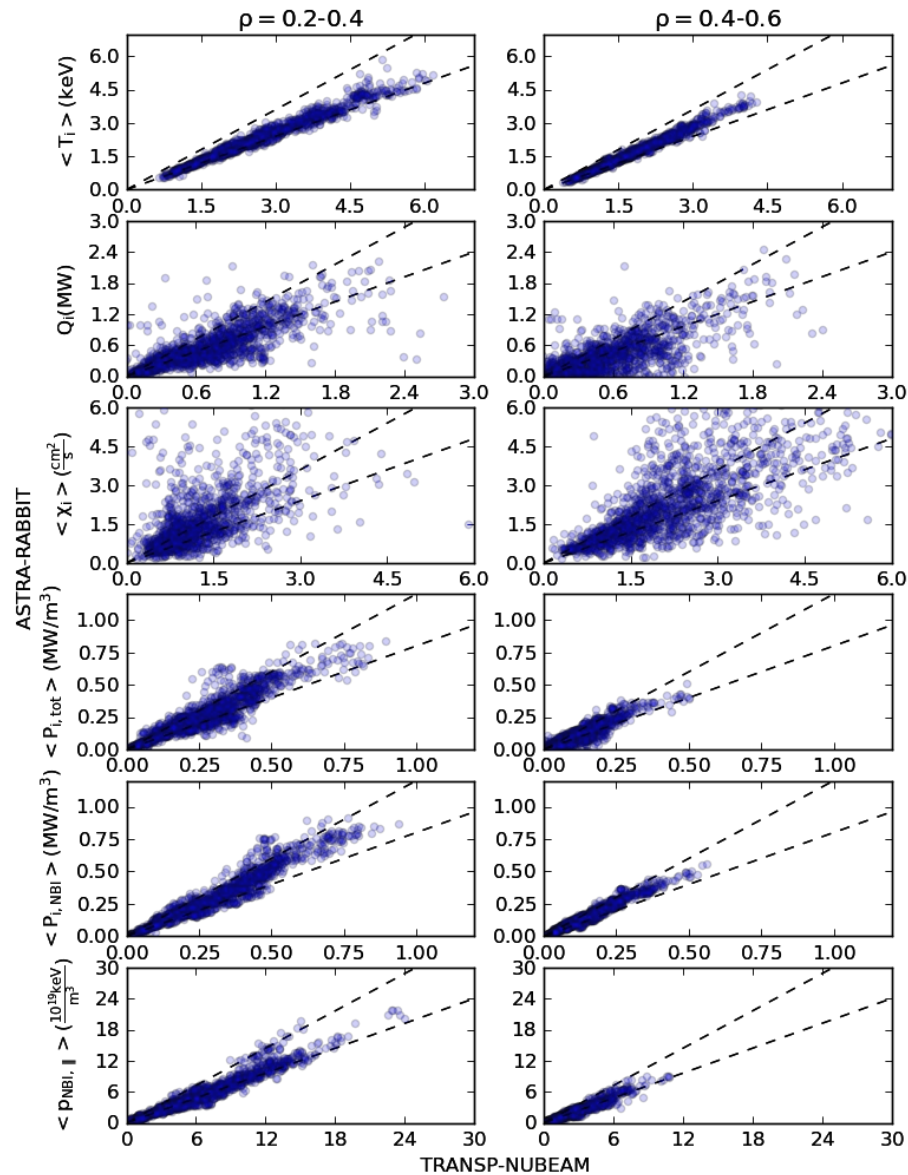
Encoded state at any time in future is linear function of the initial state and the trajectory of actuators

Model-Predictive Control:

$$\text{Minimize } (z - z_{target})^T Q (z - z_{target}) + u^T R u$$

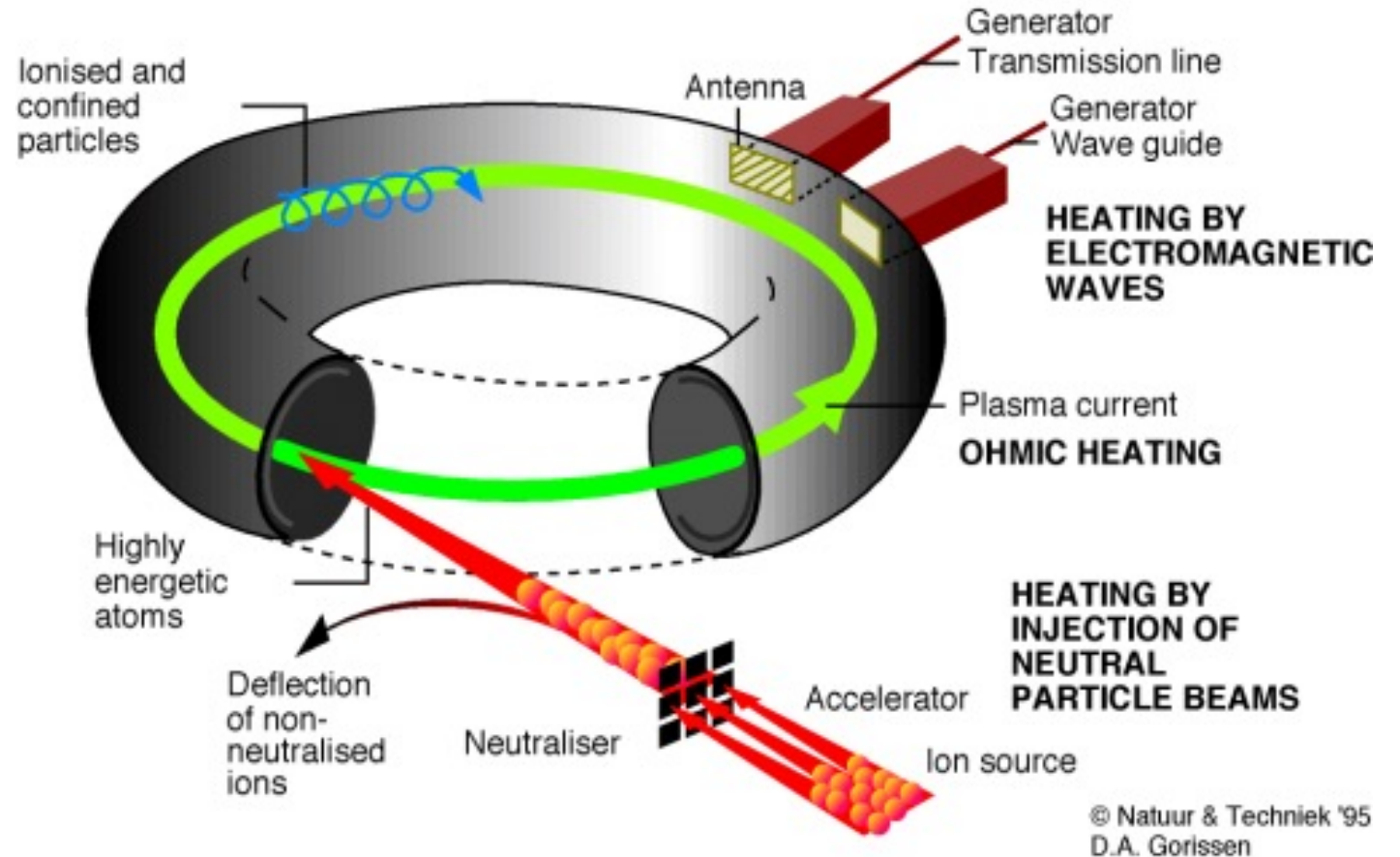
$$\text{s.t. } Du < d$$

More details on ASTRA/TRANSP comparison



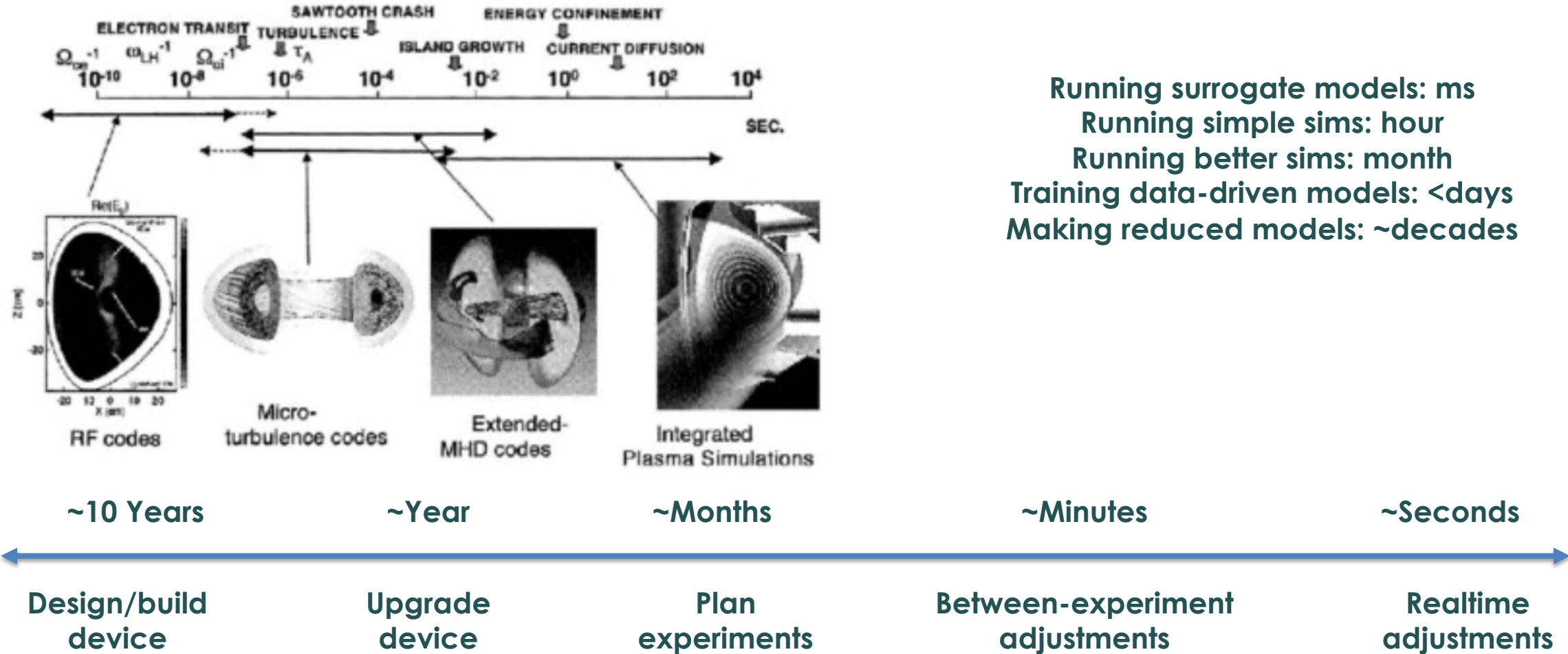
Kinetic plasma profile actuators

- **Total neutral beam power**
- **Total neutral beam torque**
- **Total ECH power**
- **Target plasma current**
- **Total deuterium gas puffed**
- **Target toroidal magnetic field**
- **Target plasma shape parameters**



Timescales

Relevant timescales for a burning plasma experiment



1st+2nd author publications

Cross-verification and validation of predictive capabilities of the ASTRA and TRANSP codes

Abbate, Fable et al *Physics of Plasmas* [in review]

Created a novel benchmark (an empirical model) for validation and for the first time compared ASTRA 8

Towards LLMs as Operational Copilots for Fusion Reactors

Mehta, Abbate et al *2023 NeurIPS Workshop AI4Science* [in review]

Applied large language models in a retrieval augmented generation system to assist tokamak operators. Deployed as a bot in the DIII-D tokamak operations Discord, and on an MIT server for the Alcator C-Mod tokamak.

A general infrastructure for data-driven control design and implementation in tokamaks

Abbate, Conlin et al *2023 Journal of Plasma Physics* 89(1) 895890102

Deployed the model below in a model-predictive framework on DIII-D (using finite set control) to achieve user-specified pressure and temperature profiles by varying injected power and torque.

Offline Model-Based Reinforcement Learning for Tokamak Control

Char, Abbate et al *2023 Learning for Dynamics and Control Conference*

Trained similar model but with uncertainty output and more robust long-time dynamics, deployed in reinforcement learning controller at DIII-D to achieve user-specified betan by varying beam power

Real-Time and Adaptive Reservoir Computing With Application to Profile Prediction in Fusion Plasma

Jalalvand, Abbate et al, *2022 IEEE Transactions on Neural Networks and Learning Systems* vol. 33 no. 6

Rebuilt the model using Reservoir Computing Networks for realtime adaptability and towards a linear statespace

Data-driven profile prediction for DIII-D

Abbate, Conlin et al *2021 Nuclear Fusion* 61 046027

Developed a first-of-its-kind fully data-driven machine learning model to simulate plasma dynamics